

Electron-boson coupling: Beyond the equilibrium interpretation

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PRB 87, 235139 (2013)
PRB 90, 075126 (2014)
arXiv:1505.07055 (updated tomorrow)

***APS March Meeting,
March 7, 2016***



M.A. Sentef (MSPD)



J.K. Freericks (Georgetown)



B. Moritz, T.P. Devereaux (Stanford/SLAC)



J.D. Rameau, P.D. Johnson (BNL)



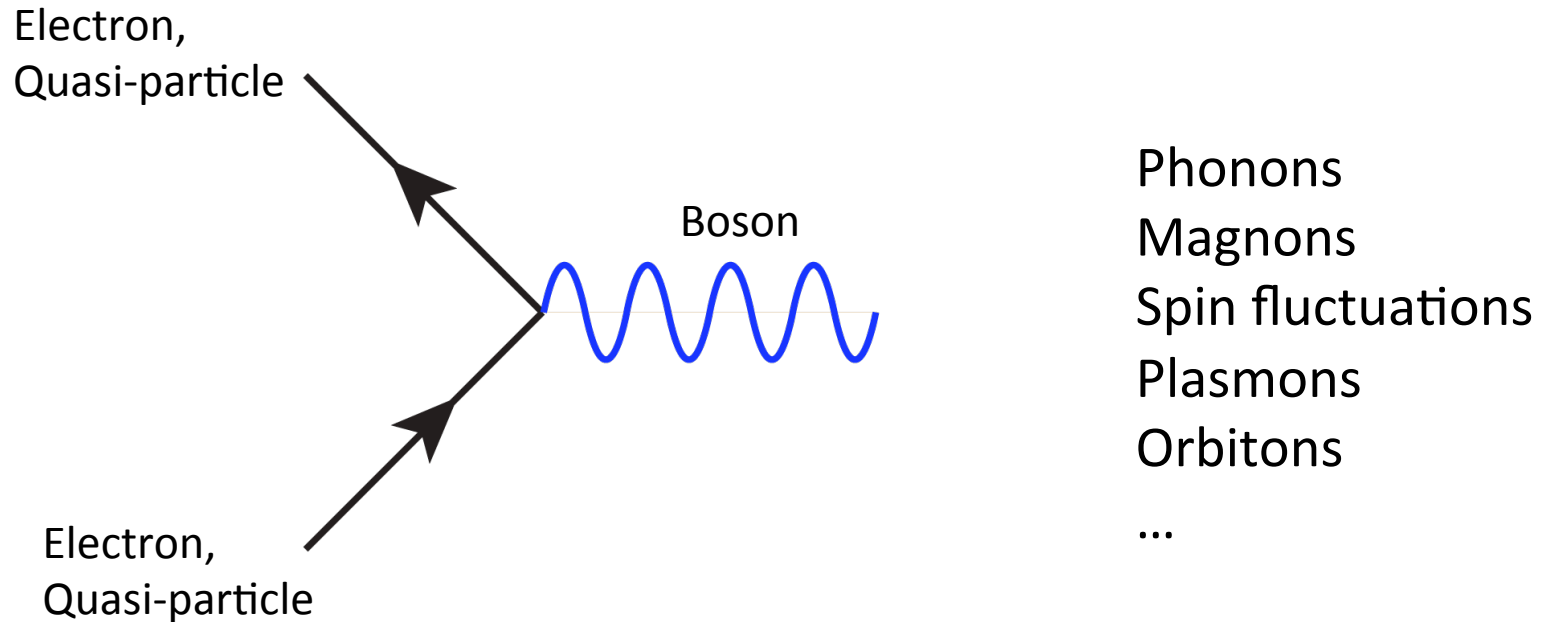
**S. Freutel, M. Ligges, I. Avigo, U. Bovensiepen
(Duisburg-Essen)**



Electron-boson coupling: Beyond the equilibrium interpretation

- Electron-boson coupling in cuprates
- Boson interactions and population decay rates
- Violation of Matthiessen's rule in the time domain

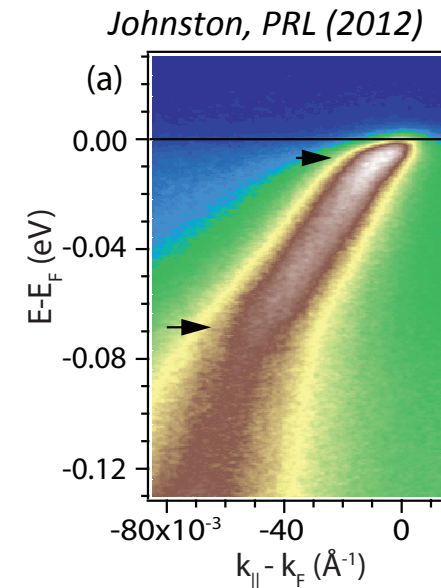
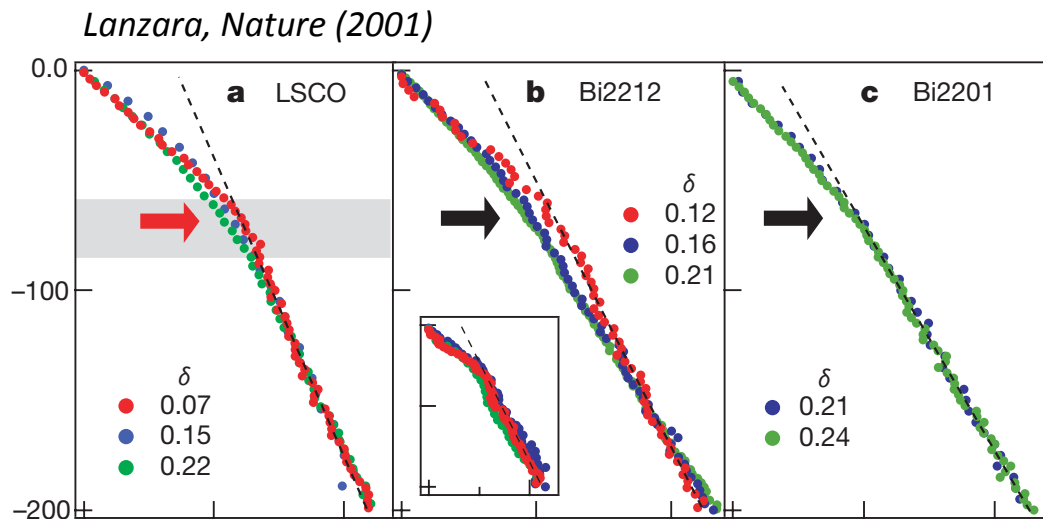
Electron-boson coupling



$$H = \sum_{\mathbf{k}} \epsilon(\mathbf{k}) c_{\mathbf{k}}^{\dagger} c_{\mathbf{k}} + \sum_{q} \Omega_q b_q^{\dagger} b_q + \sum_{\mathbf{k}q} g_{\mathbf{k},q}^2 c_{\mathbf{k}+q}^{\dagger} c_{\mathbf{k}} (b_q + b_{-q}^{\dagger})$$

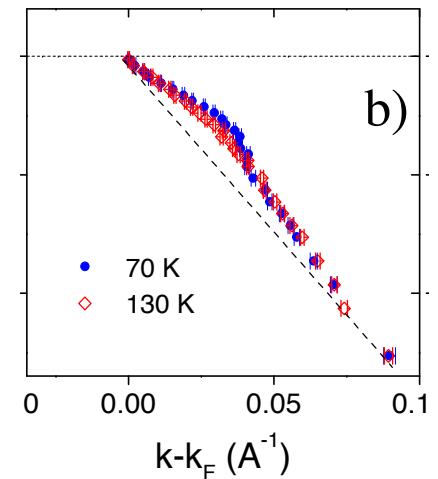
Electrons
Bosons
Electron-boson coupling

Kinks in the quasiparticle dispersion

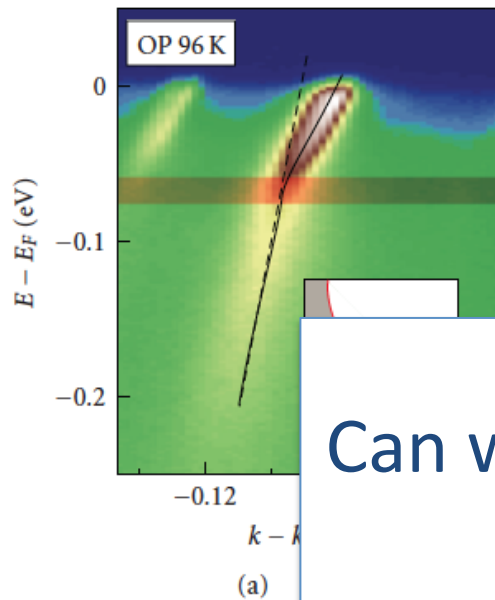


- Indications of coupling to bosons
 - Origin?
 - Effects on quasiparticles

Johnson, PRL (2001)



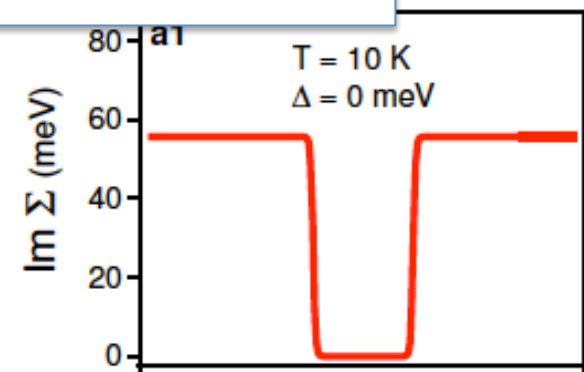
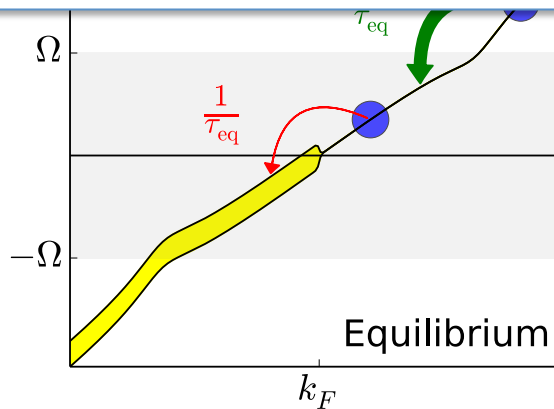
Manifestations of electron-boson interactions in spectra



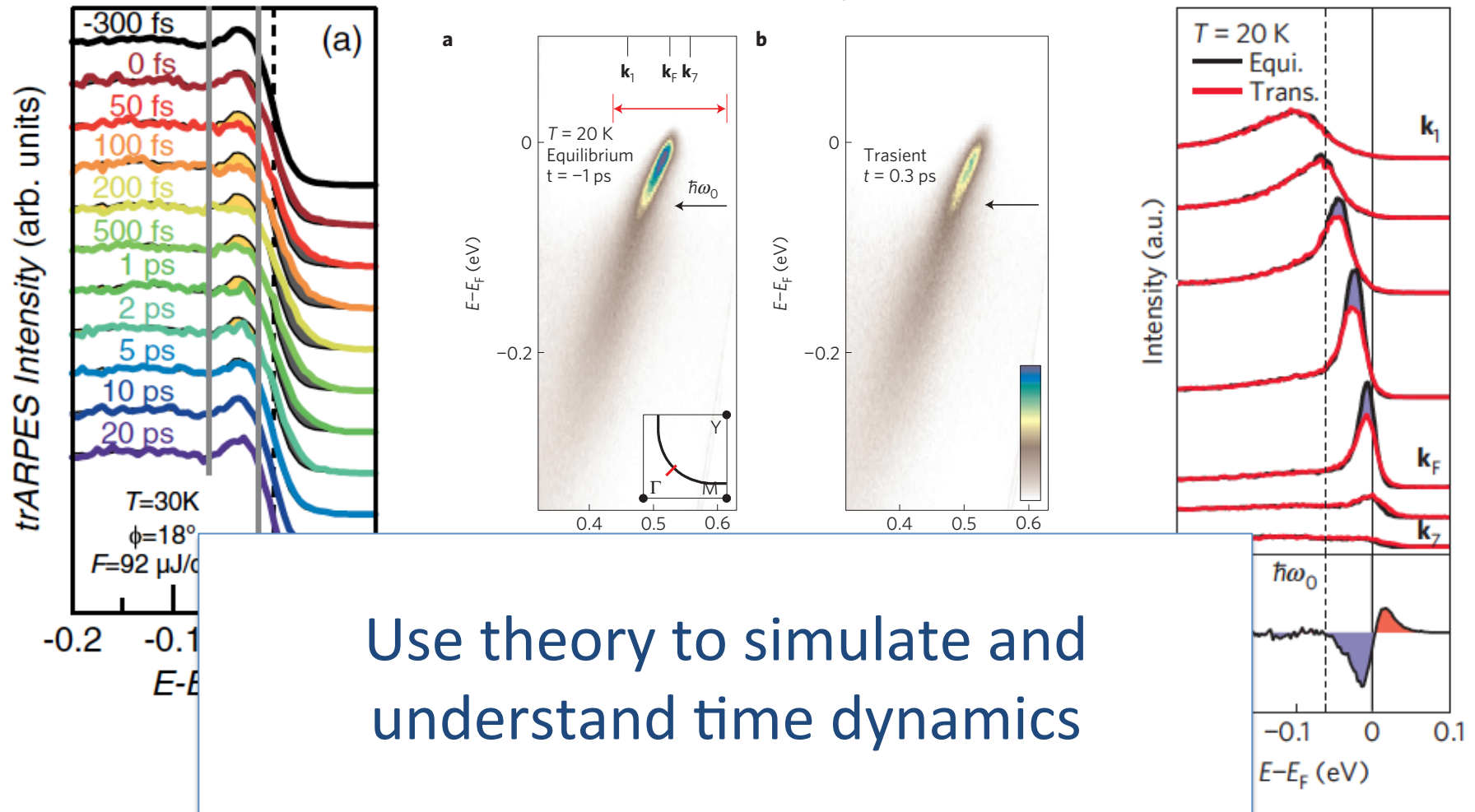
Kinks in dispersion

→ coupling to bosonic modes
(phonons, spin fluctuations, ...)

Can we measure lifetimes τ directly in the time domain?



Manifestations of electron-boson interactions in time-resolved spectra



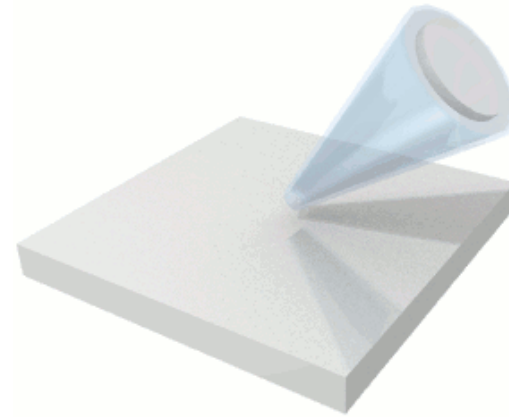
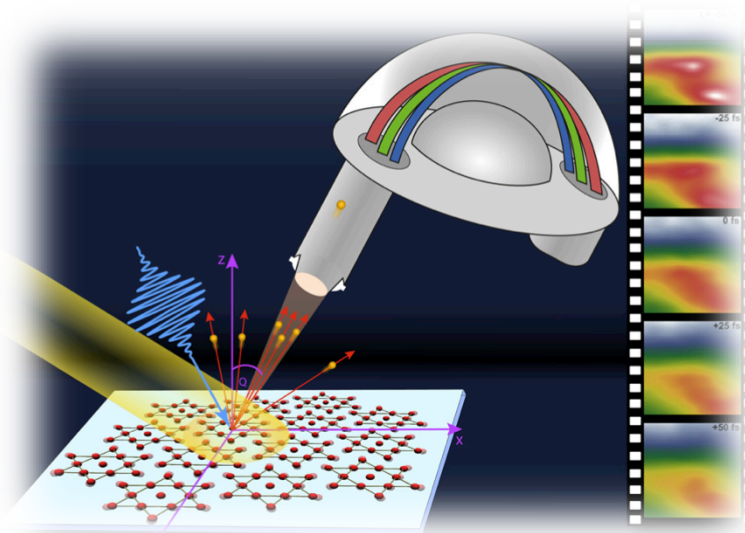
Use theory to simulate and understand time dynamics

Electron-boson coupling: Beyond the equilibrium interpretation

- Electron-boson coupling in cuprates
- Boson interactions and population decay rates
- Violation of Matthiessen's rule in the time domain

- Time- and angle-resolved photoemission spectroscopy

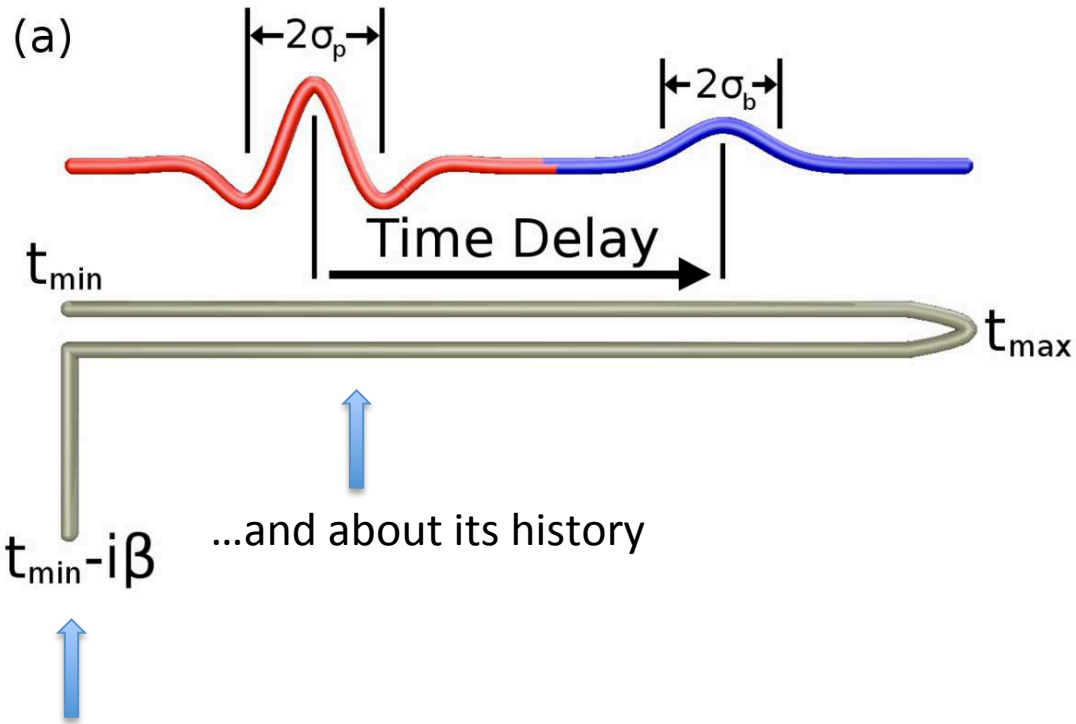
Image courtesy
of J. Harms,
University of
Hamburg



- (1) Incoming light pulse (the pump) excites electrons and lattice
- (2) Second incoming light pulse (the probe) ejects electrons (called photoemission) some time Δt later
- (3) Excited electrons are measured as a function of their energy and momentum

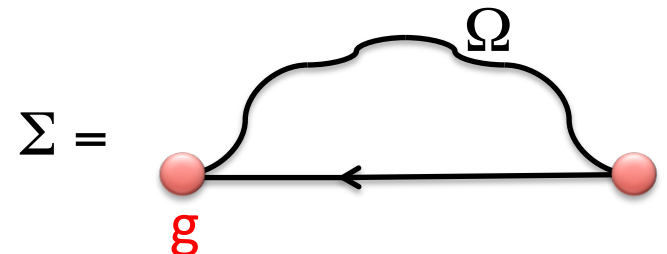
Non-Equilibrium Keldysh Formalism

$$G_{\mathbf{k}}(t_2, t_1; \omega) = G_{\mathbf{k}}^0(t_2, t_1; \omega) + \int dt_1 \int dt_2 G_{\mathbf{k}}^0(t_2, t_1; \omega) \Sigma(t_1, t_2) G_{\mathbf{k}}(t_1, t_2; \omega)$$



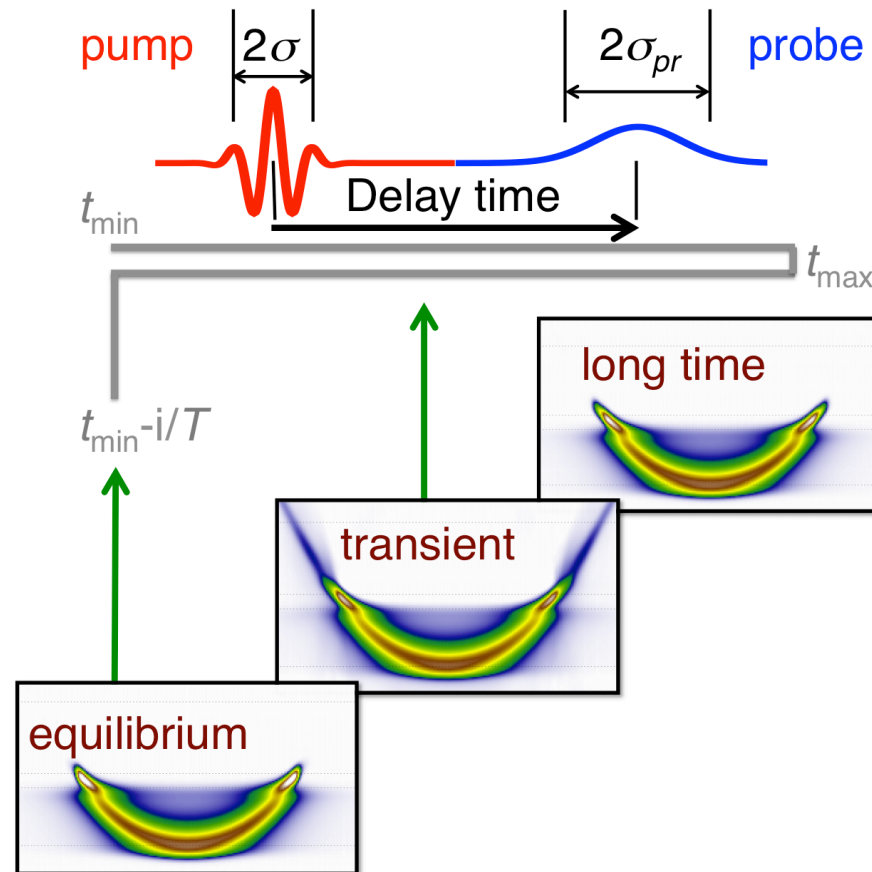
self-energy Σ :
 electron-electron scattering
 electron-phonon scattering
 ...

Include the effects of strong driving field through Peierls substitution

$$\mathbf{k} \rightarrow \mathbf{k} - e\mathbf{A}(t)$$


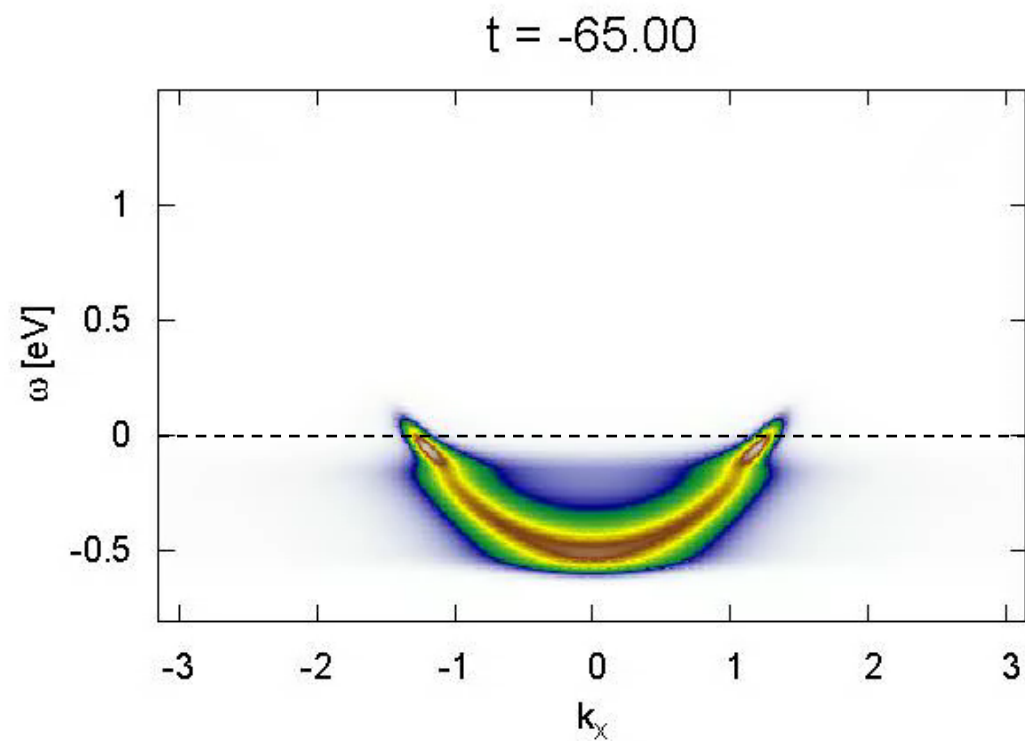
System knows about its thermal initial state...

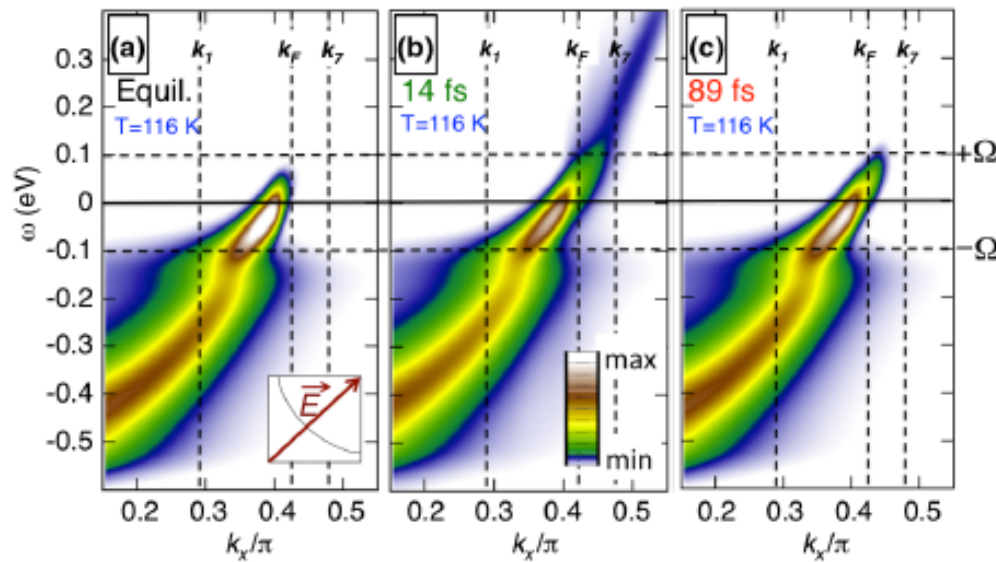
Pump-probe photoemission



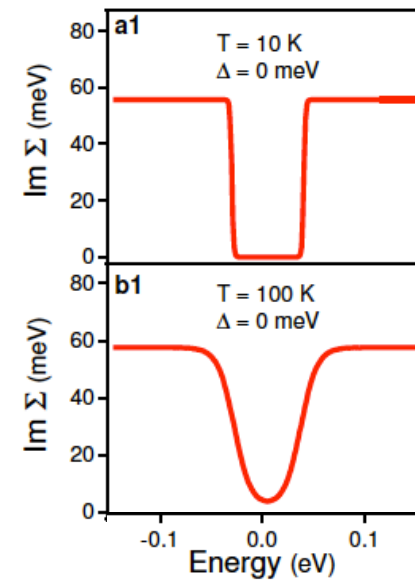
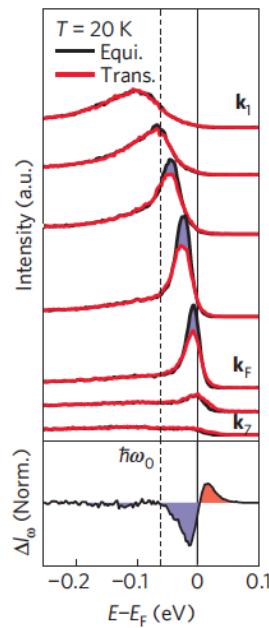
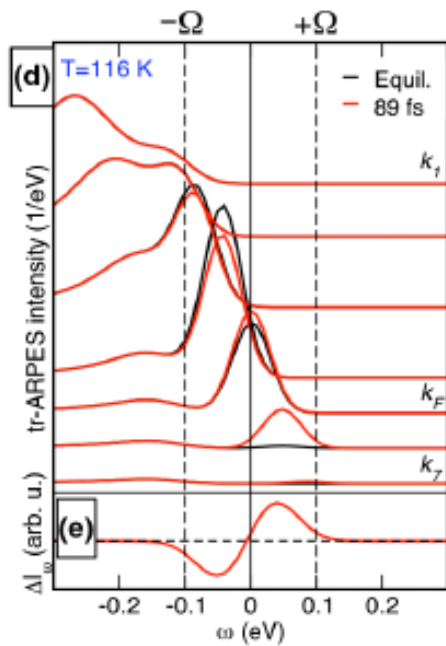
$$A_{\mathbf{k}}(\omega, t_0) = \text{Im} \frac{1}{2\pi\sigma^2} \int dt dt' G_{\mathbf{k}}^<(t, t') e^{-(t-t_0)^2/2\sigma^2} e^{-(t'-t_0)^2/2\sigma^2} e^{i\omega(t-t')}$$

Electron-lattice coupling



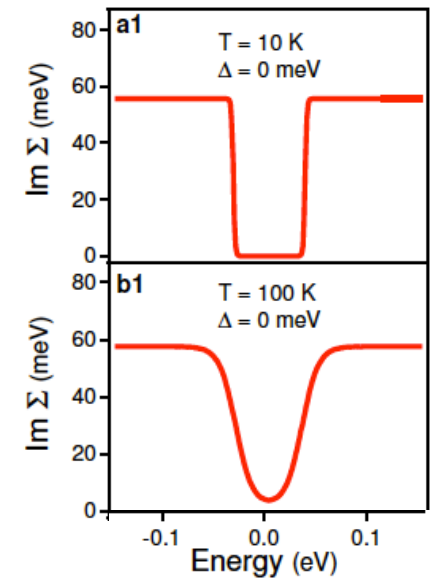
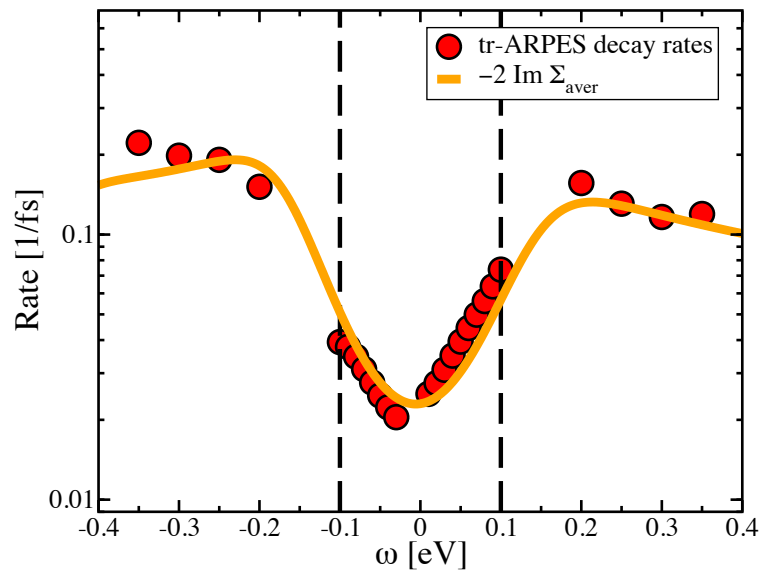
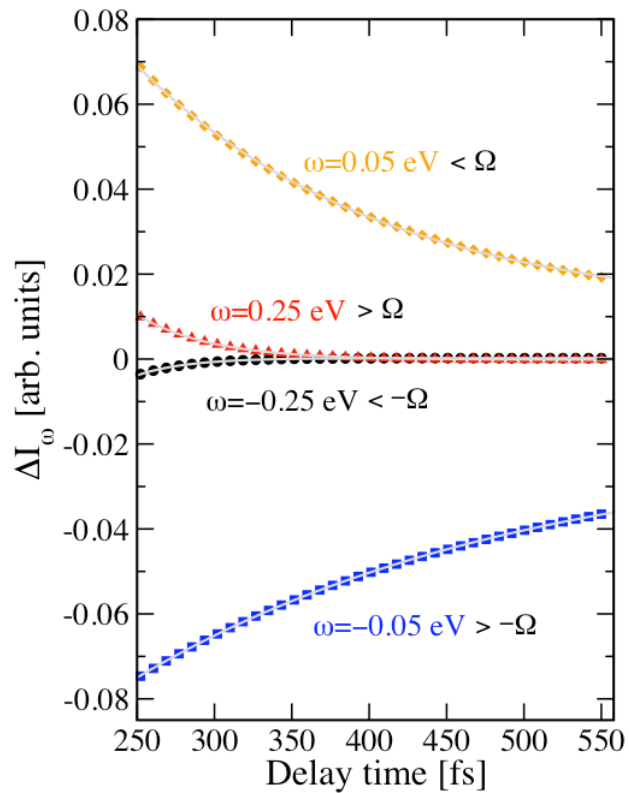


Return to equilibrium significantly slowed within a window around E_F



Electron-lattice coupling

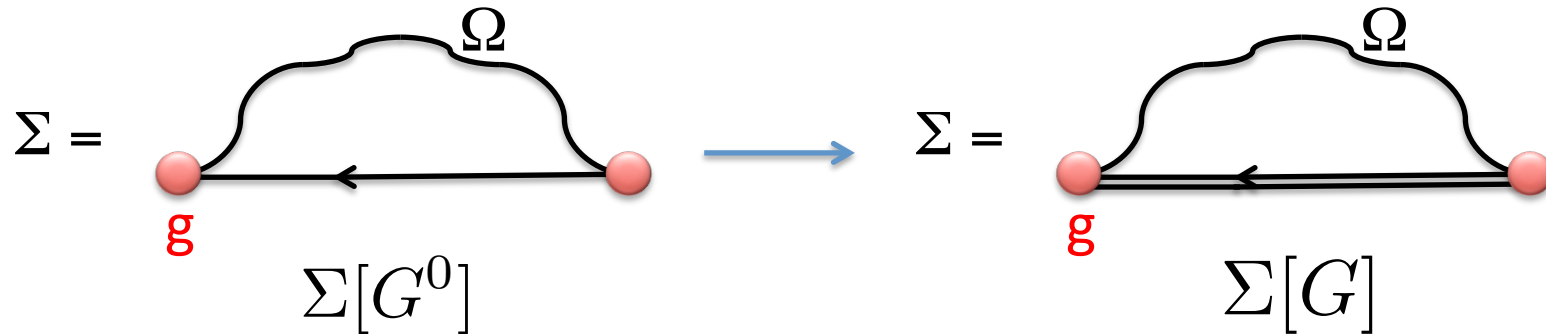
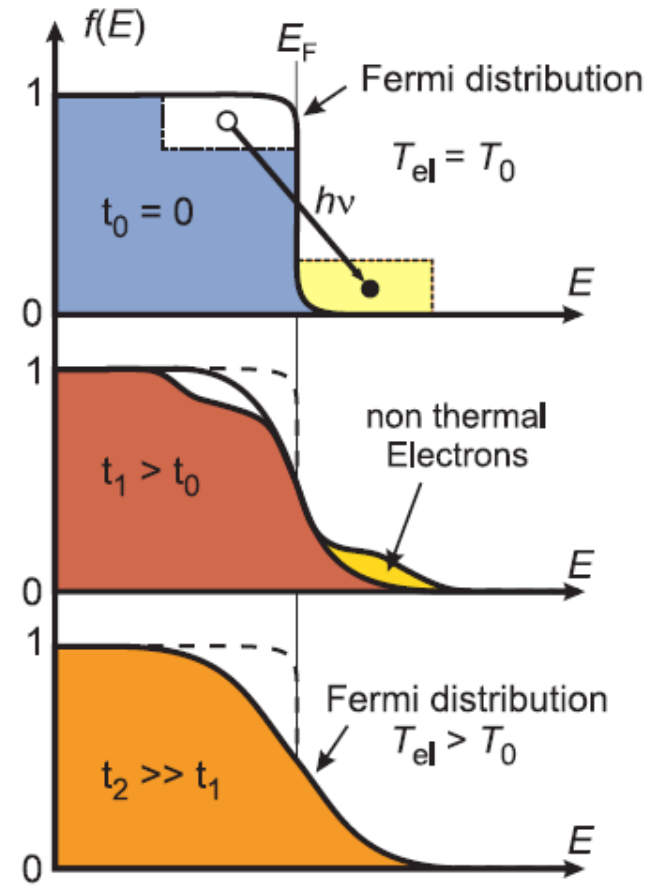
b



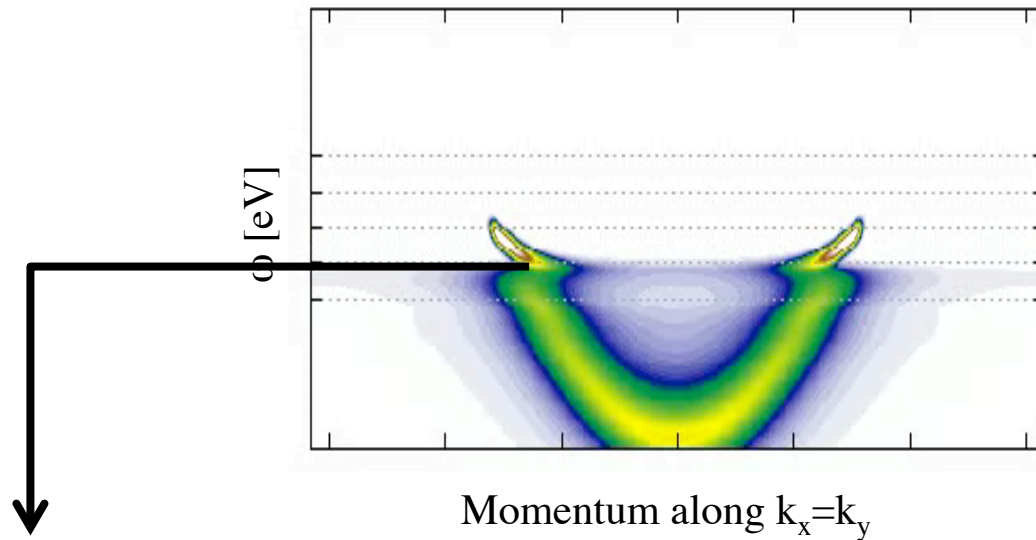
$$1/\tau(\omega)$$

How does the pump fluence affect these results?

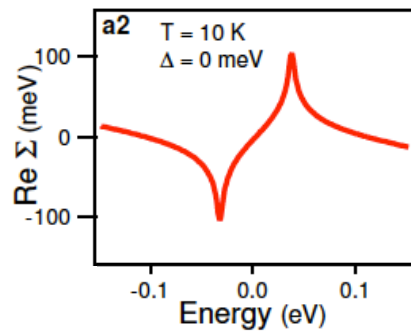
We should account for the changes in the distribution self-consistently.



Driving beyond the weak limit

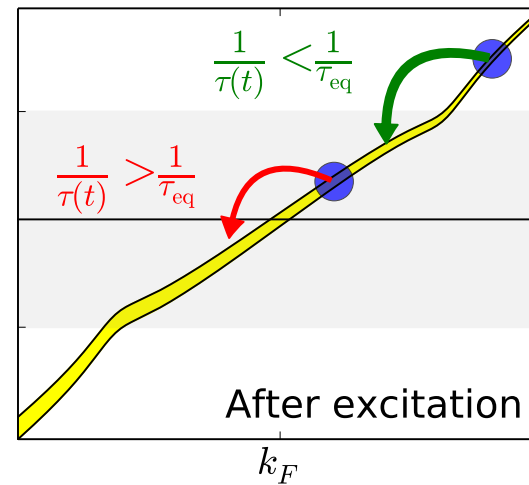
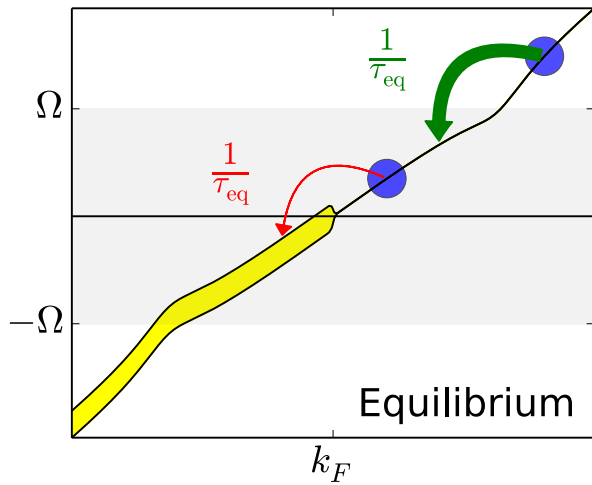
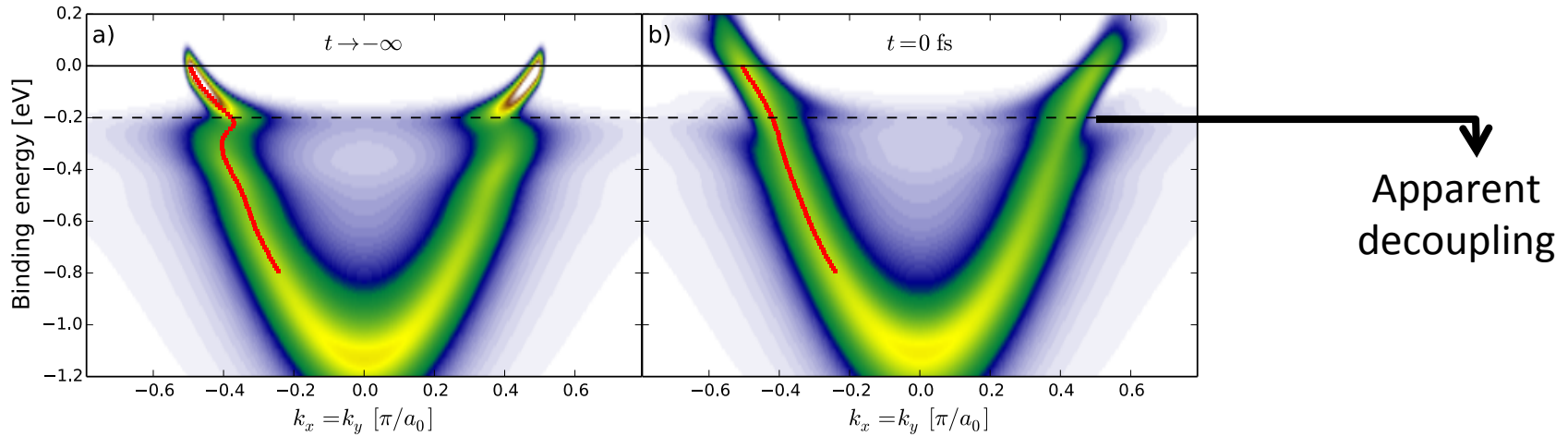


Sharp kink is a signature of large electron-boson coupling

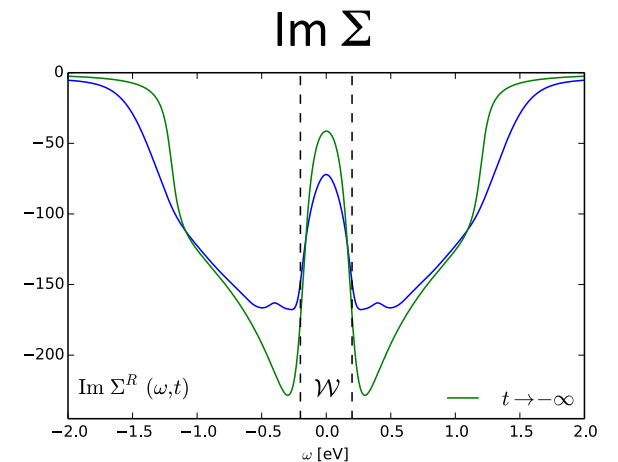
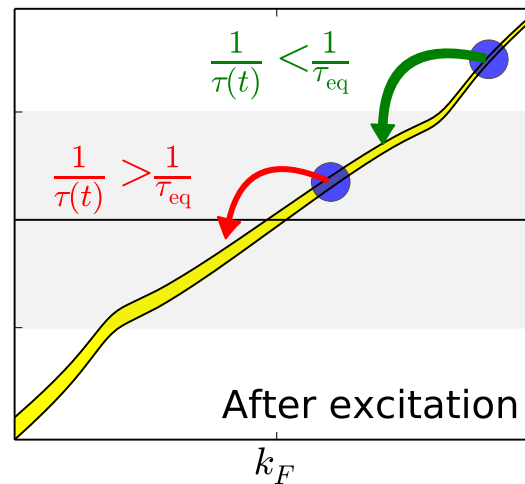
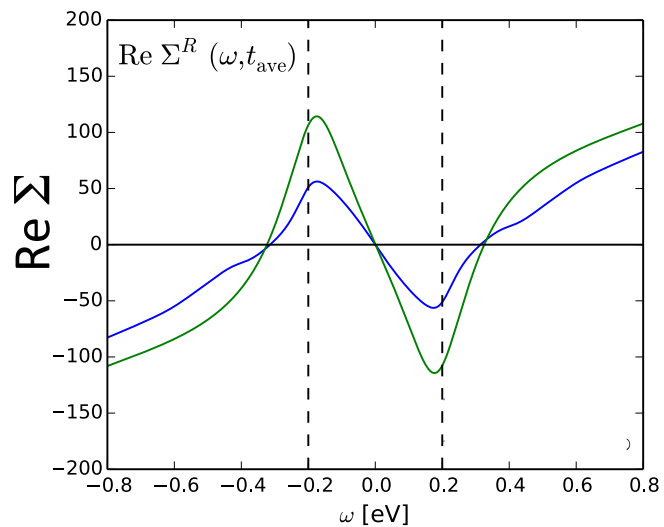
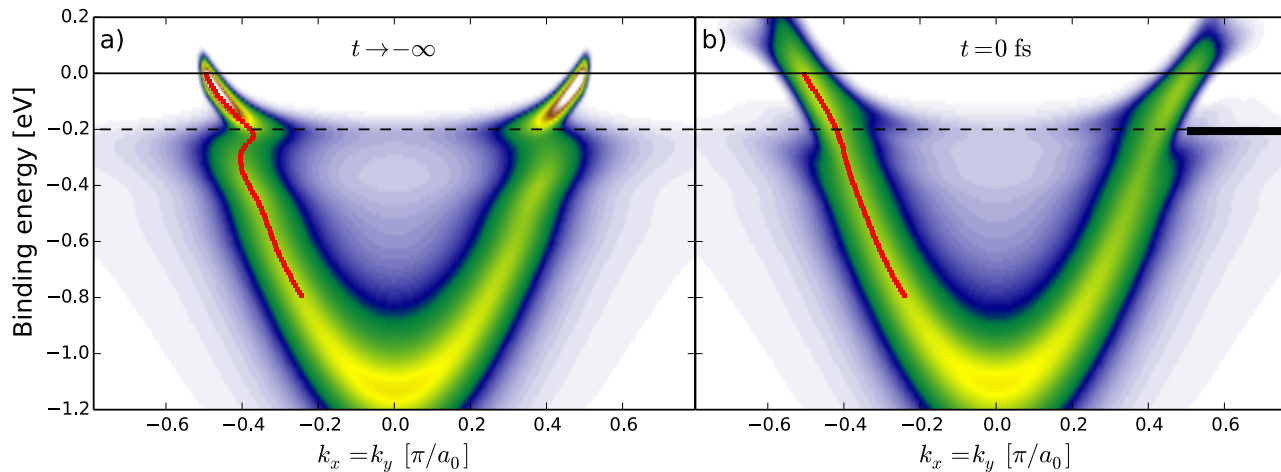


Strong excitation appears to change features of electron-phonon coupling

Driving beyond the weak limit

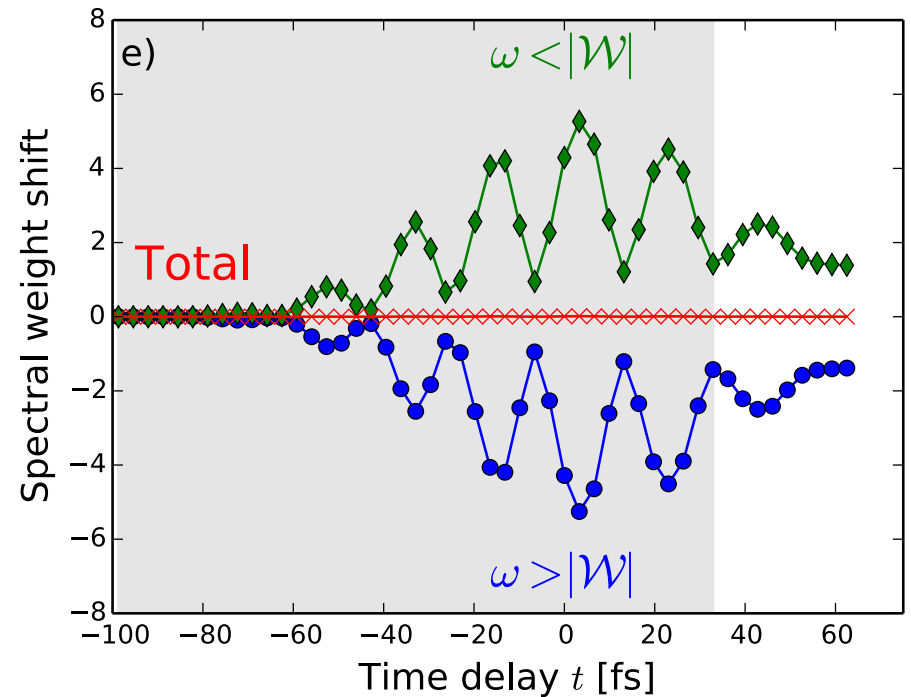
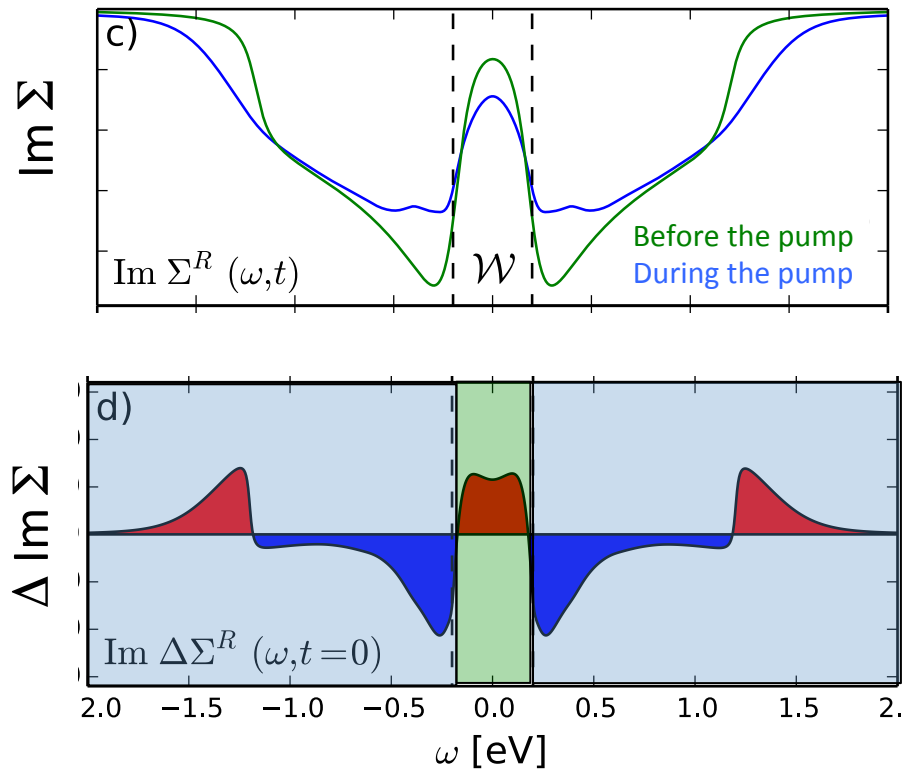


Driving beyond the weak limit



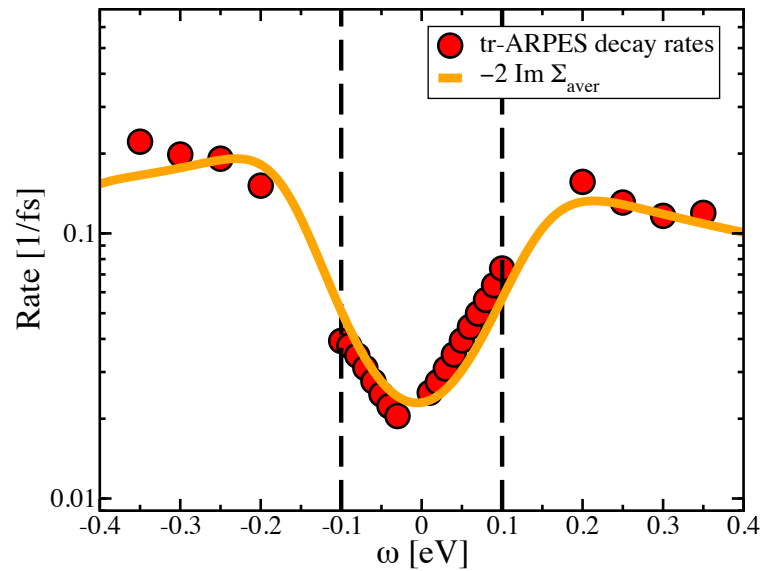
Driving beyond the weak limit

Interaction spectral weight shifts

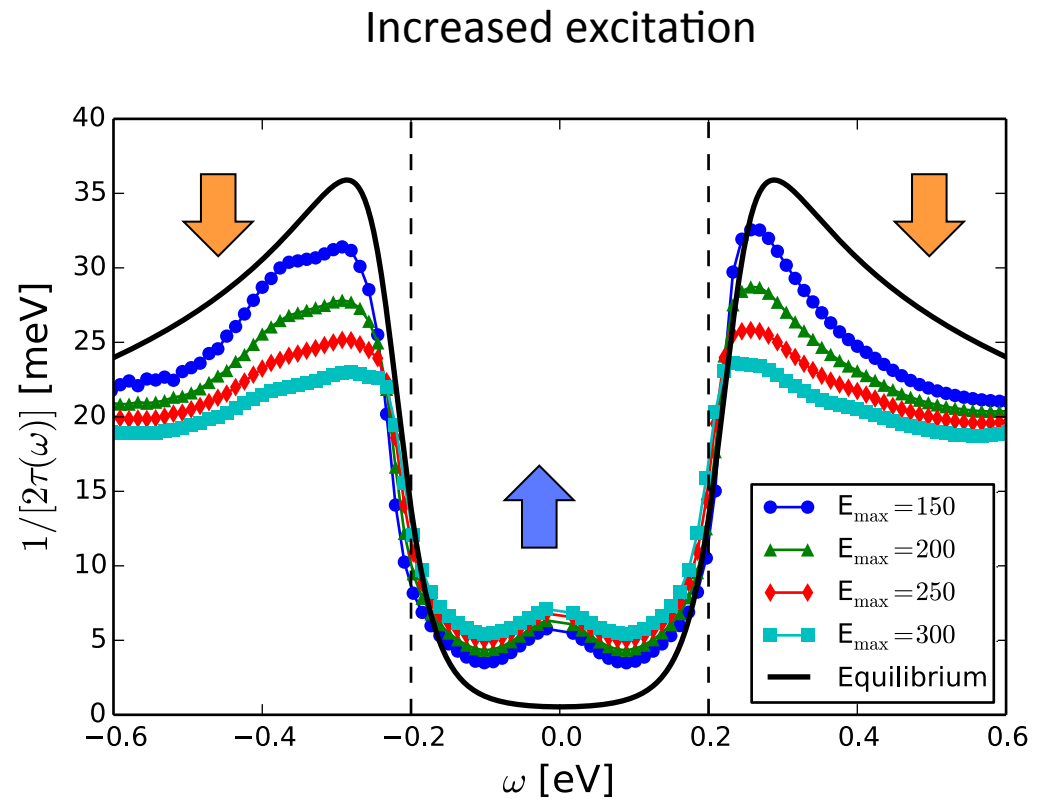


Total interaction stays constant!

Driving beyond the weak limit



Low fluence limit
Phys. Rev. X 3, 041033

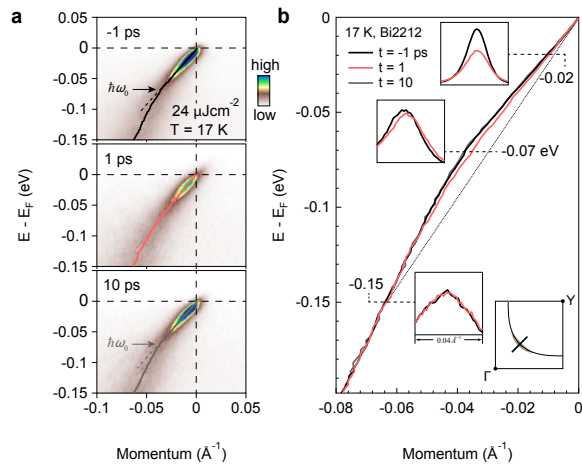


Strong pumping leads to fluence- and time-dependent interactions

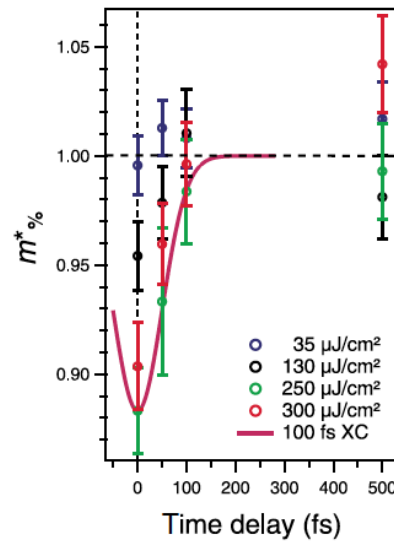
$$1/\tau(\omega) \approx -2\text{Im}\Sigma(\omega)$$

Experimental evidence for modified interactions

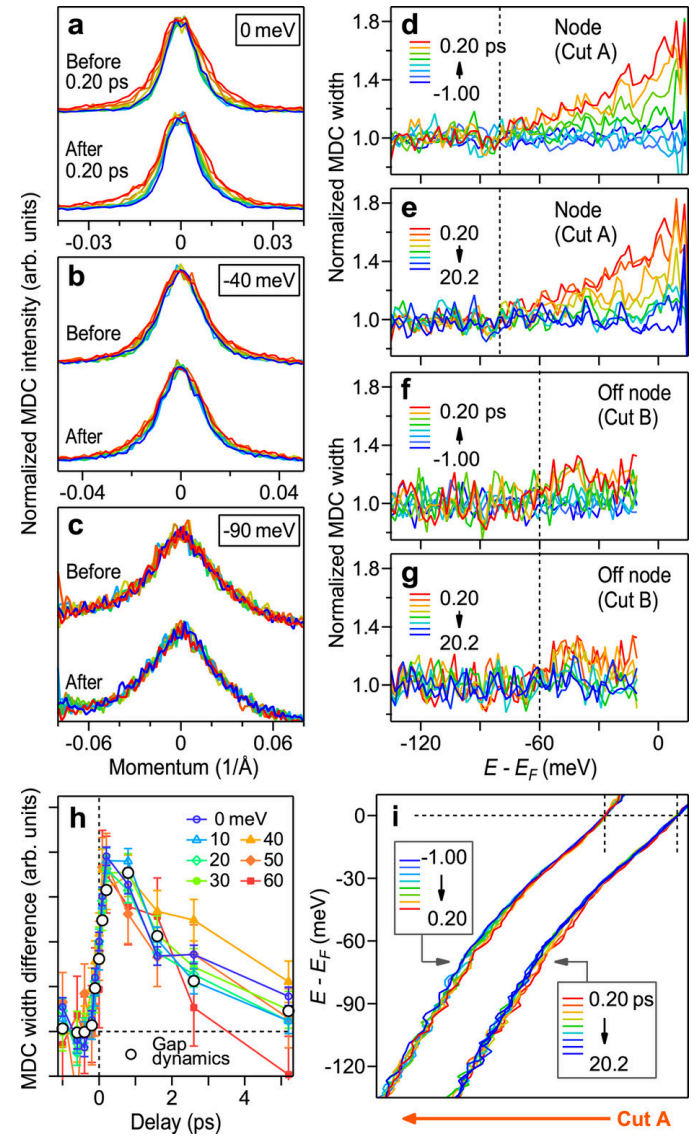
- Increase in MDC width after pumping within phonon window
- Weakening of the kink



Zhang, Nature Comm. (2014)

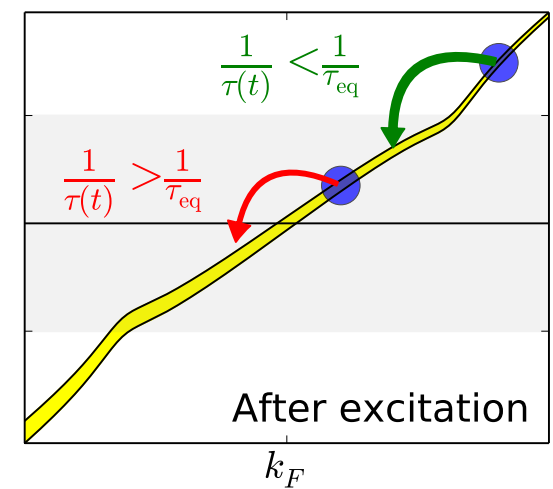
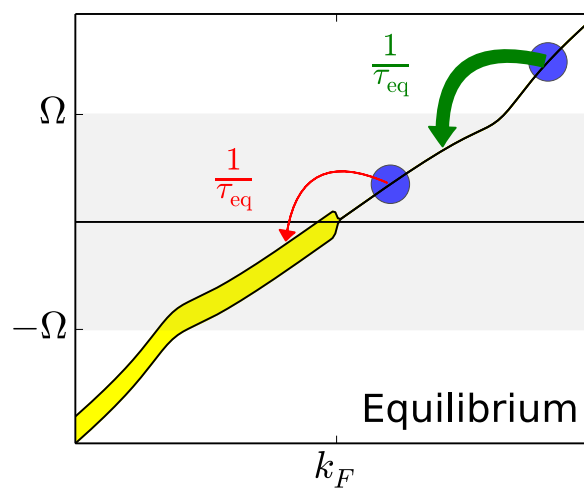
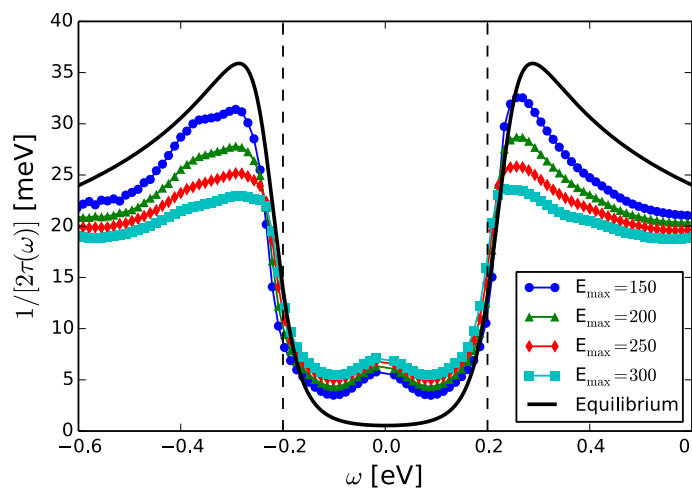
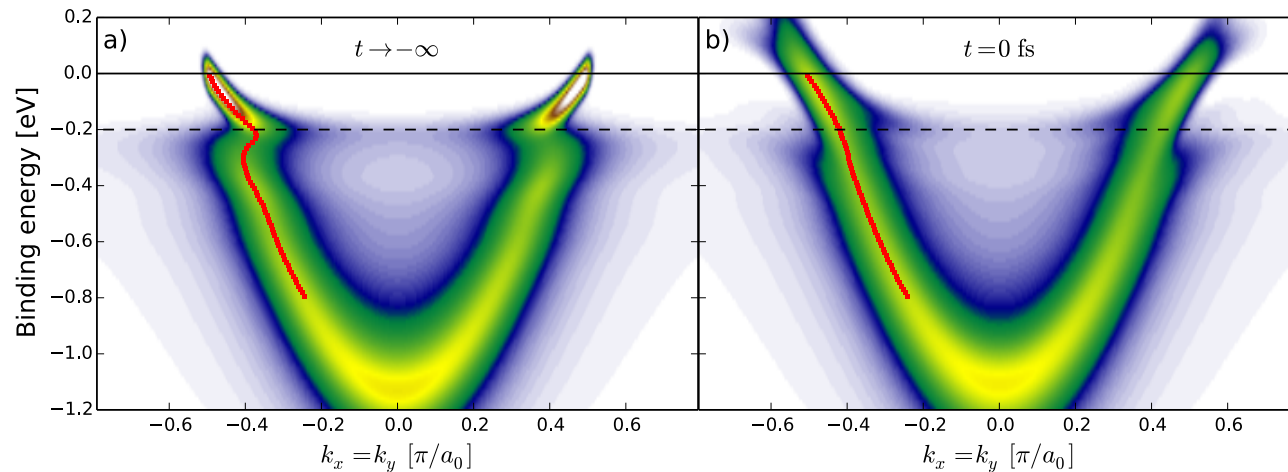


Rameau, PRB (2014)



Ishida, Nat. Sci. Reports (2016)

Changes in kink, linewidth, and population decay rate after pumping can be understood simply by considering population redistribution

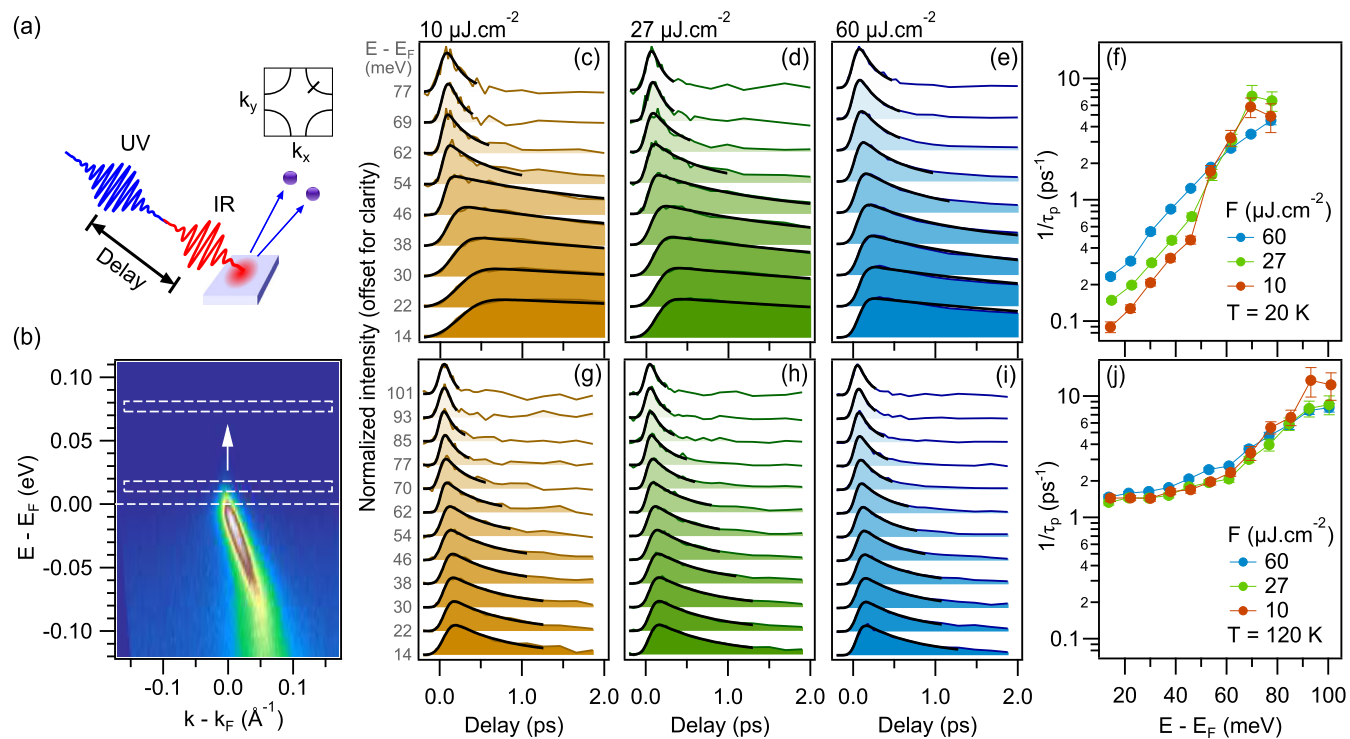


Electron-boson coupling: Beyond the equilibrium interpretation

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Inequivalence of Single-Particle and Population Lifetimes in a Cuprate Superconductor

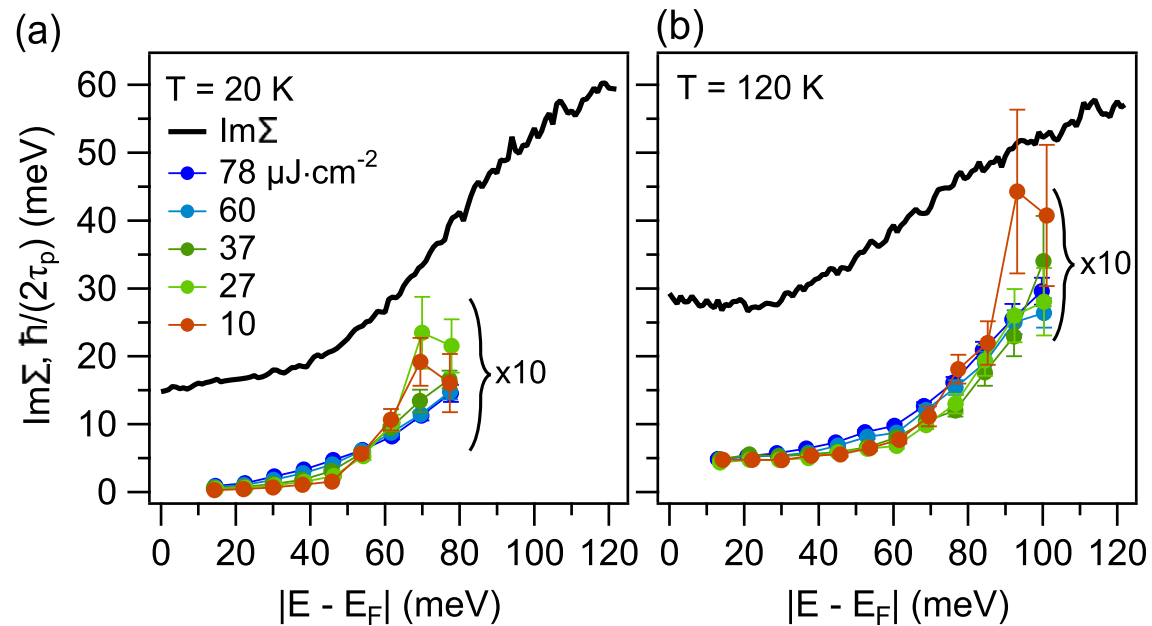
S.-L. Yang,^{1,2} J. A. Sobota,^{1,3} D. Leuenberger,^{1,2} Y. He,^{1,2} M. Hashimoto,⁴ D. H. Lu,⁴ H. Eisaki,⁵
P. S. Kirchmann,^{1,*} and Z.-X. Shen^{1,2,†}



Also: I. Gierz, S. Link, U. Starke, and A. Cavalleri, *Faraday Discuss.* 171, 311 (2014).

Inequivalence of Single-Particle and Population Lifetimes in a Cuprate Superconductor

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P. S. Kirchmann,^{1,*} and Z.-X. Shen^{1,2,†}



$$\frac{1}{\tau(\omega)} \stackrel{?}{=} -2\text{Im}\Sigma(\omega = \epsilon_{\mathbf{k}})$$

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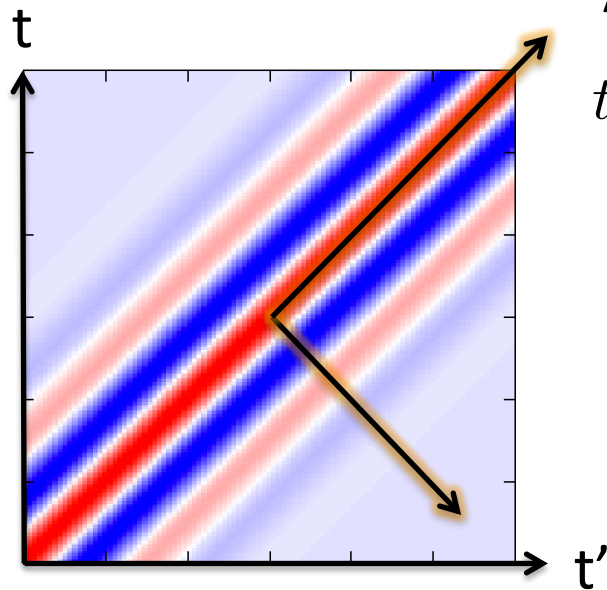


Population dynamics



Equilibrium self-energy

$$G(t, t')$$



Average time

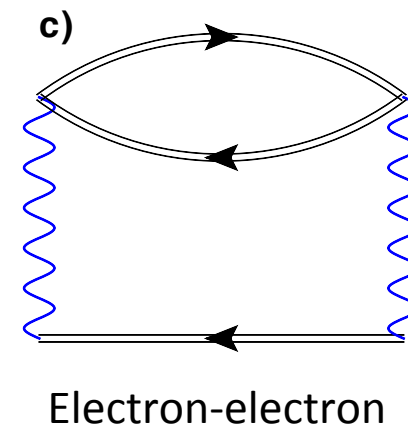
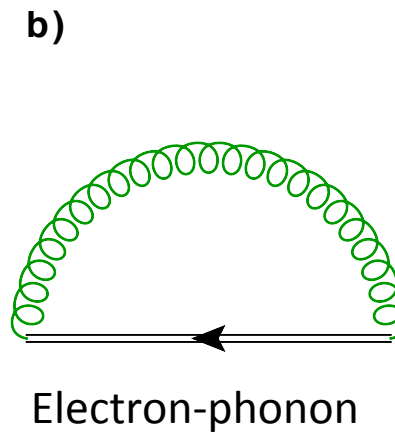
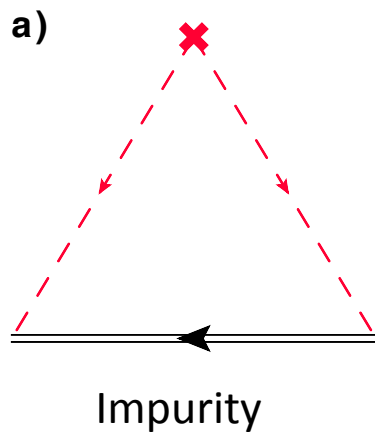
$$t_{\text{ave}} = \frac{1}{2}(t + t')$$

Relative time

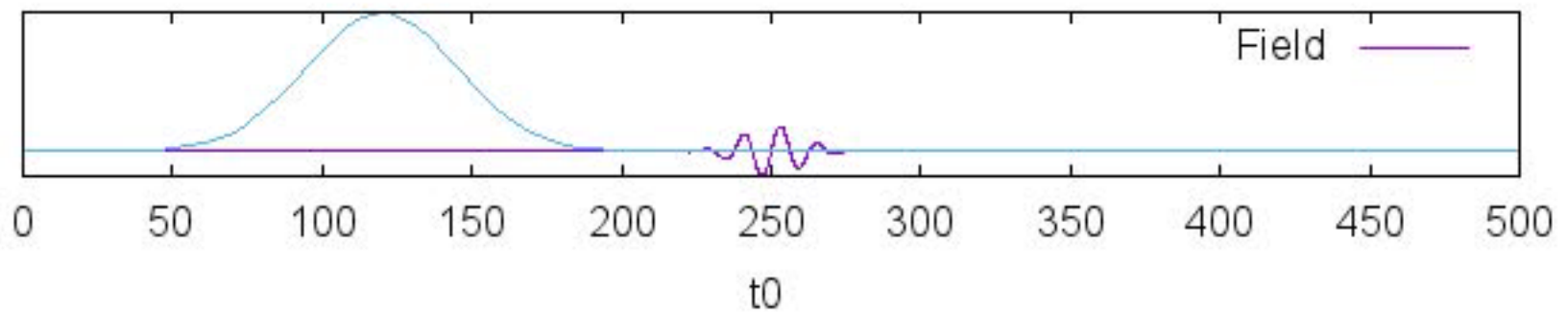
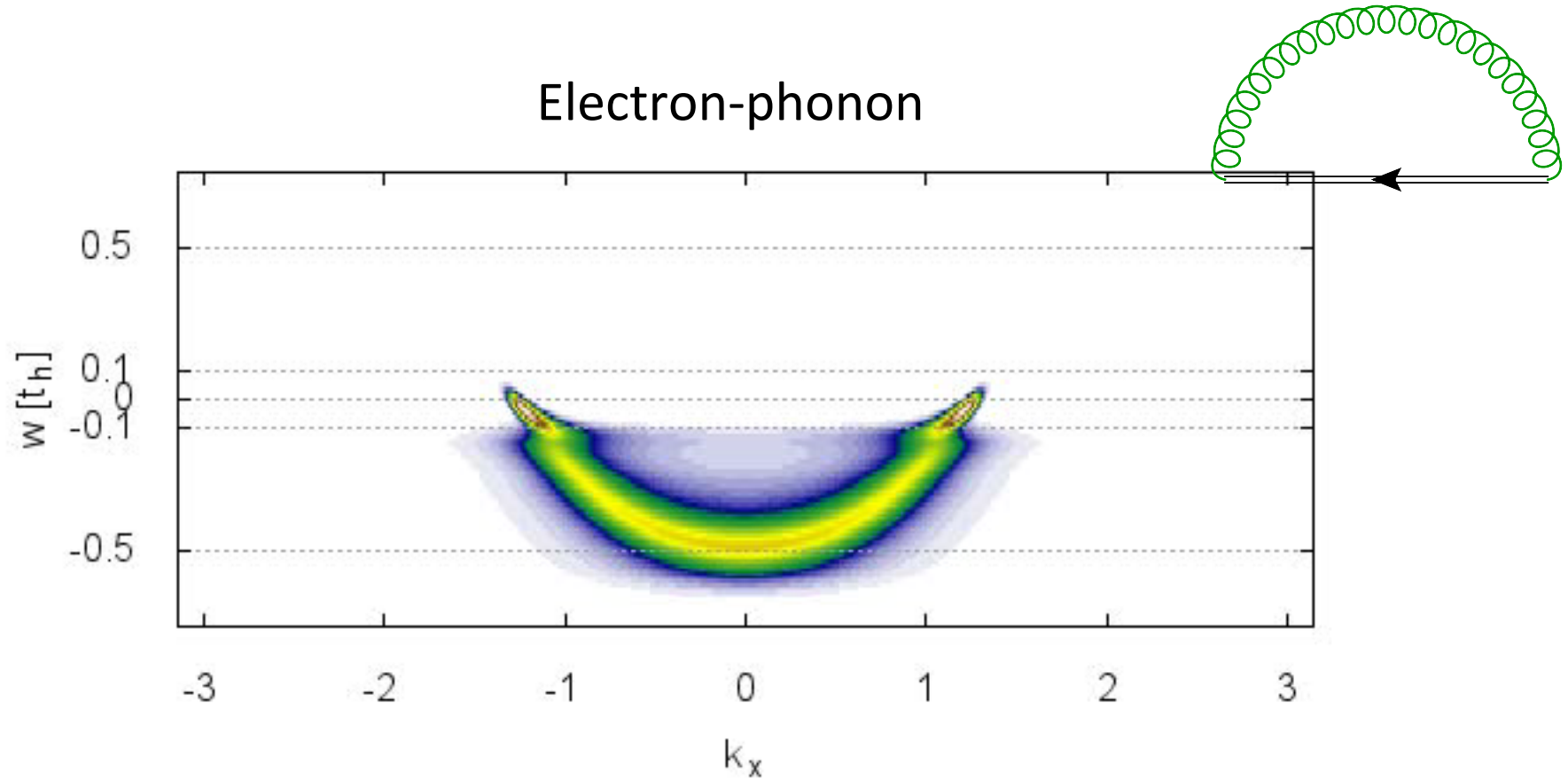
$$t_{\text{rel}} = t - t'$$

- Equilibrium frequency domain arises in $t-t'$ direction
- Population dynamics occurs along average time

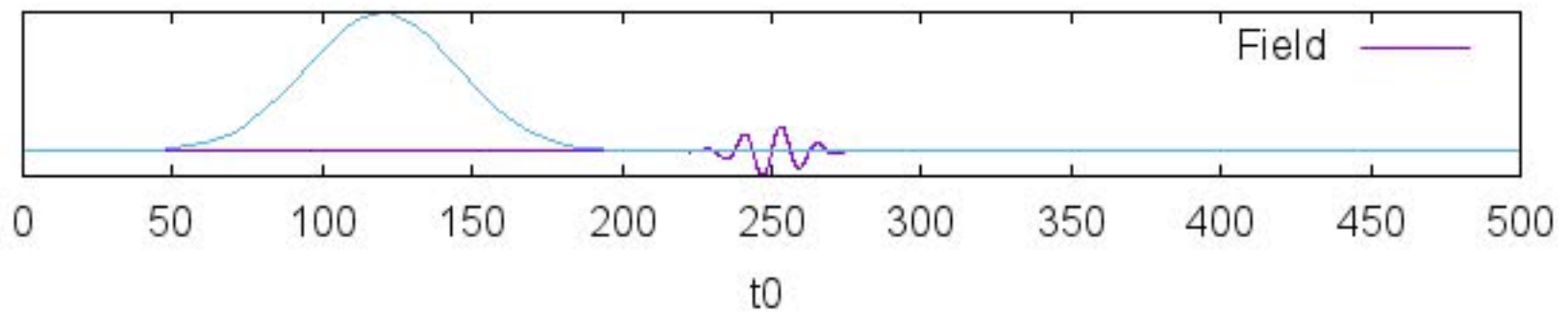
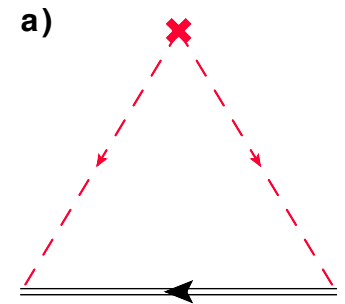
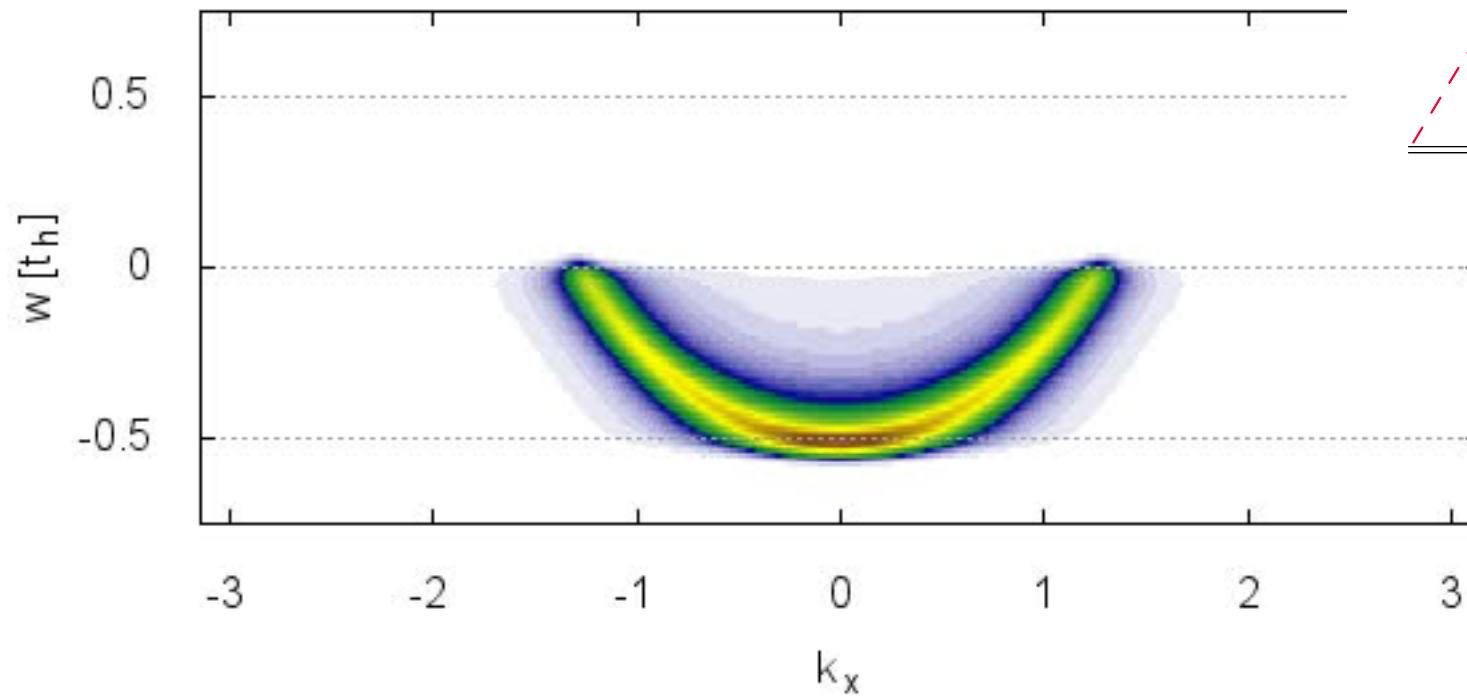
Consider interactions beyond electron-phonon coupling



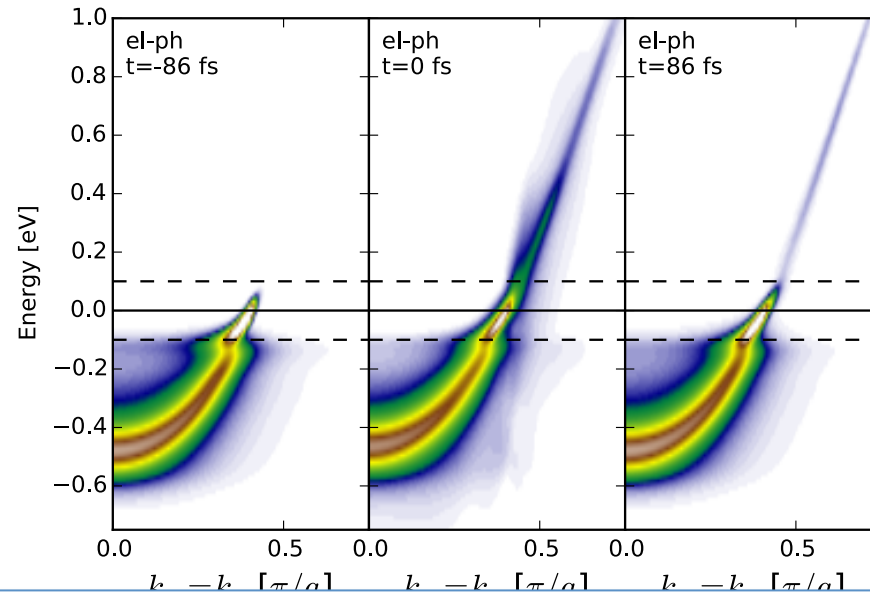
Electron-phonon



Electron-impurity

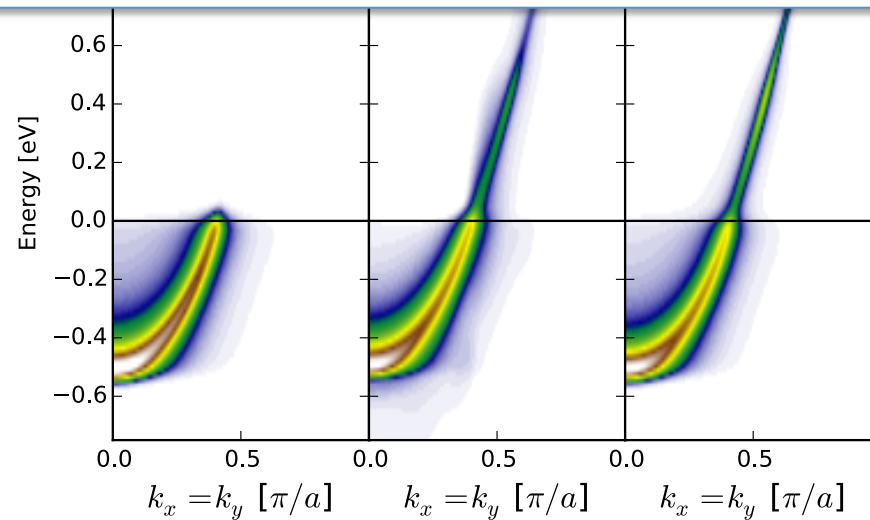


Electron-phonon



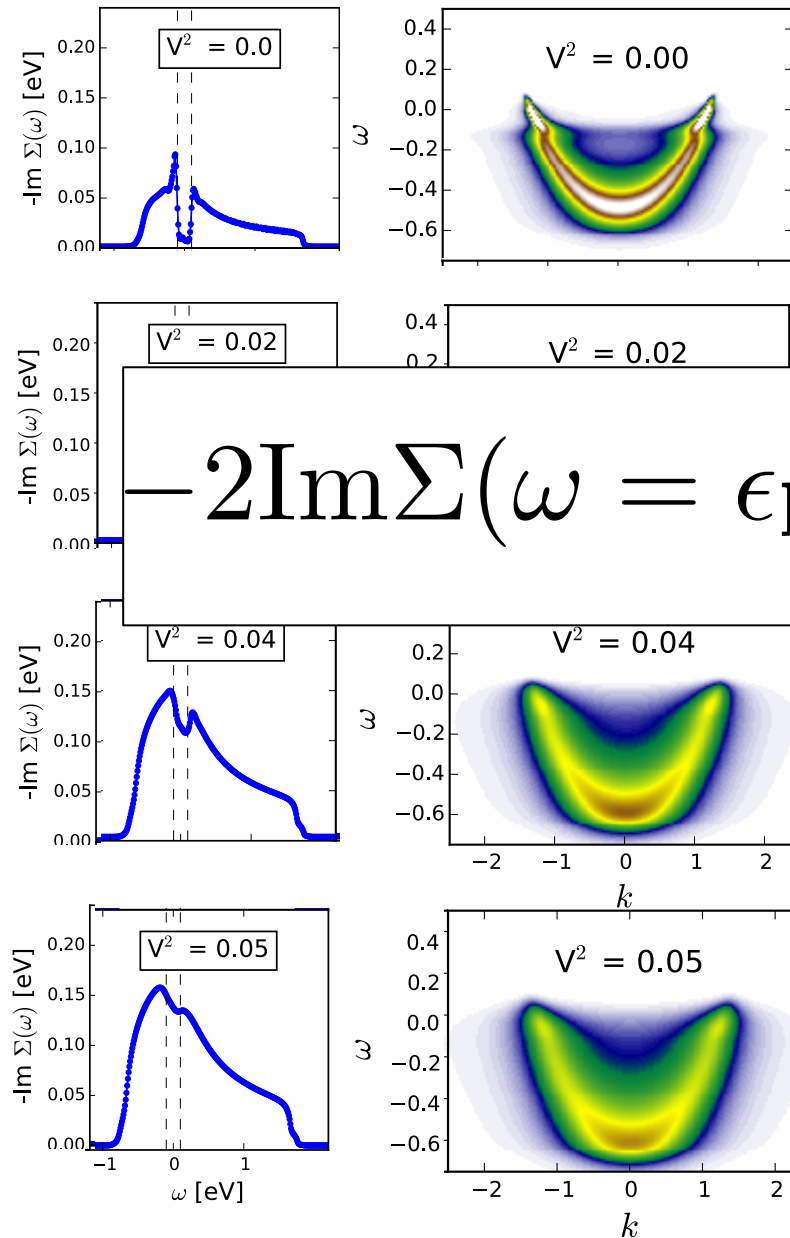
Let's consider the combination

Electron-impurity

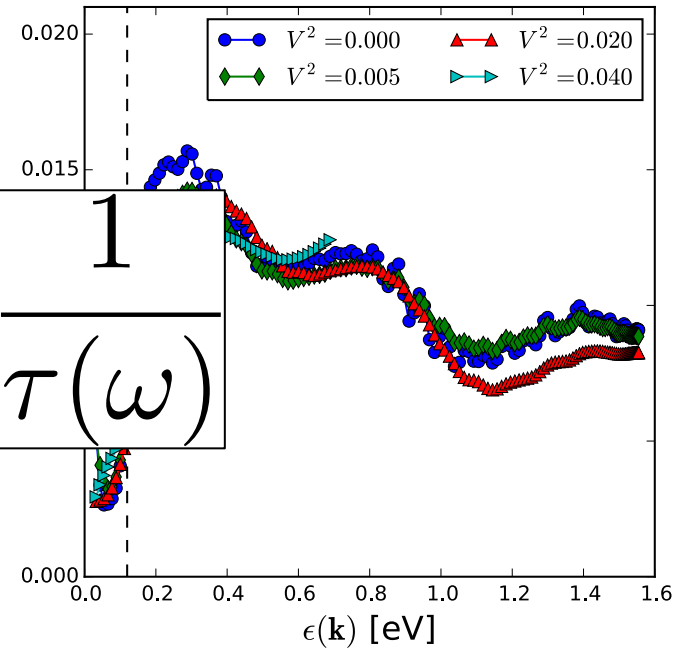


Equilibrium: quasiparticle

Non-equilibrium: population

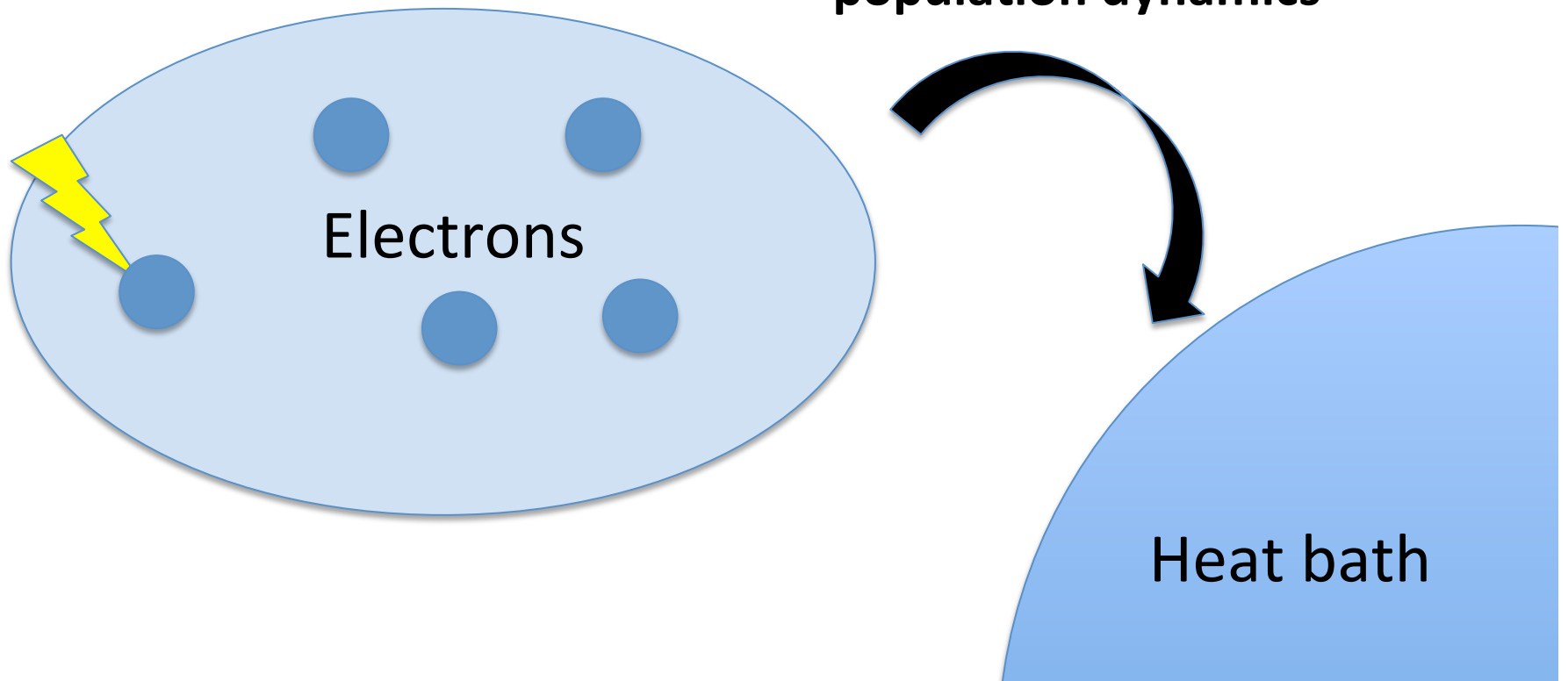


$$-2\text{Im}\Sigma(\omega = \epsilon_{\mathbf{k}}) \neq \frac{1}{\tau(\omega)}$$

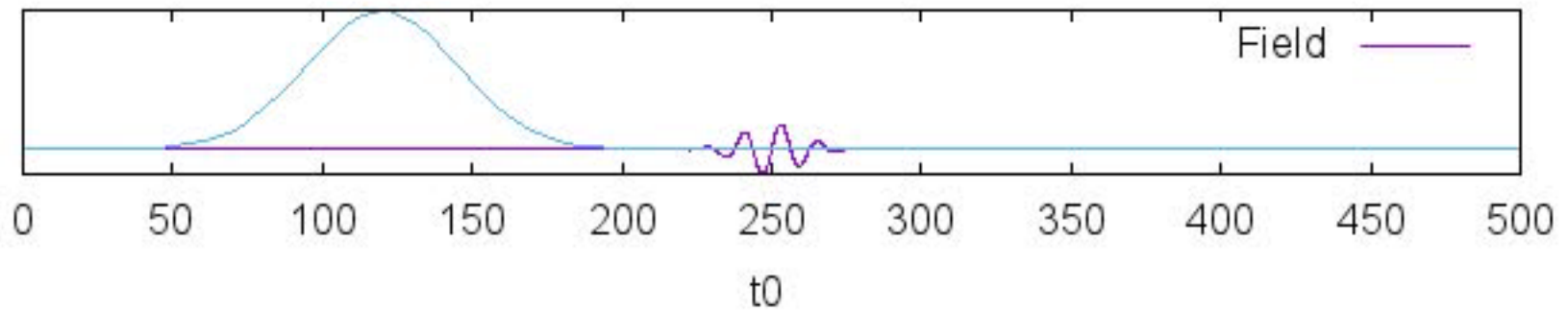
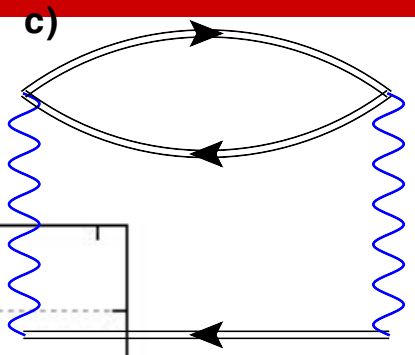
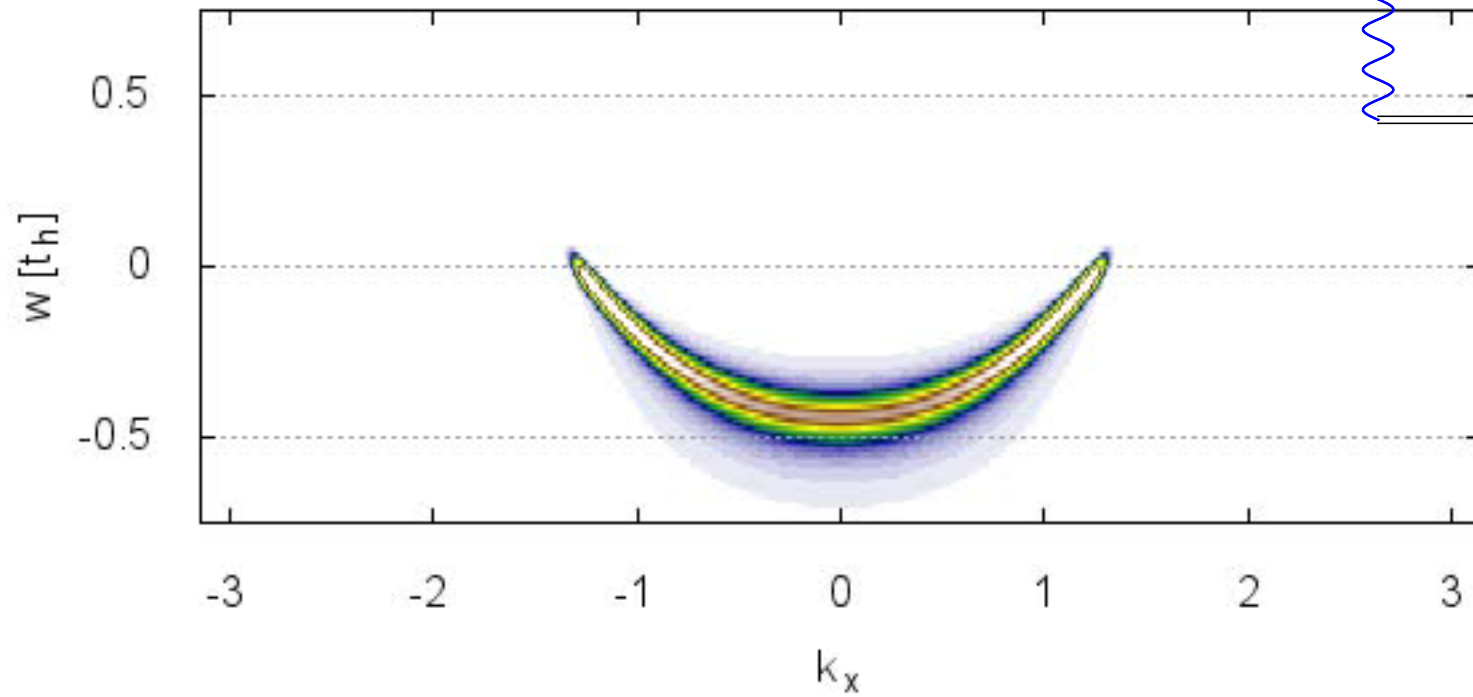


$$-2\text{Im}\Sigma(\omega = \epsilon_{\mathbf{k}}) \neq \frac{1}{\tau(\omega)}$$

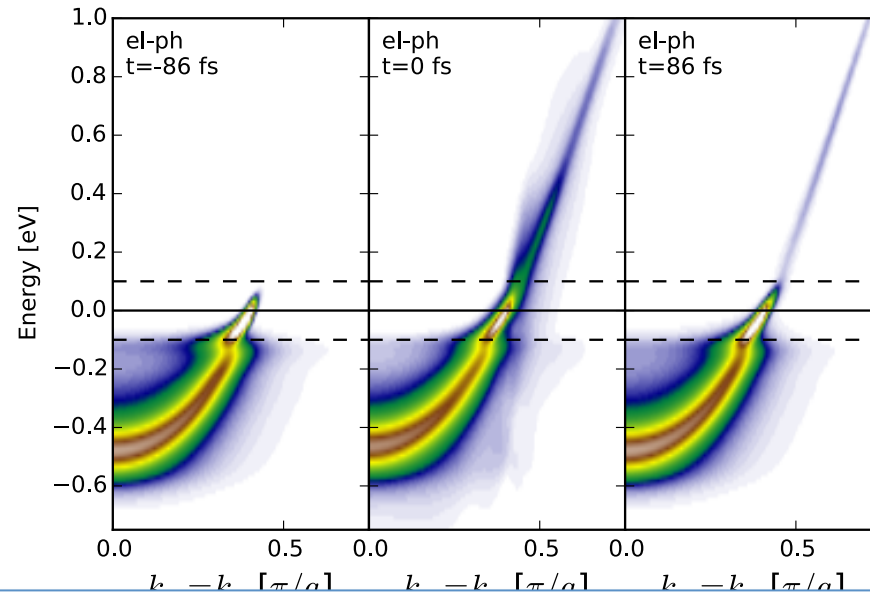
Energy transfer determines
population dynamics



Electron-electron

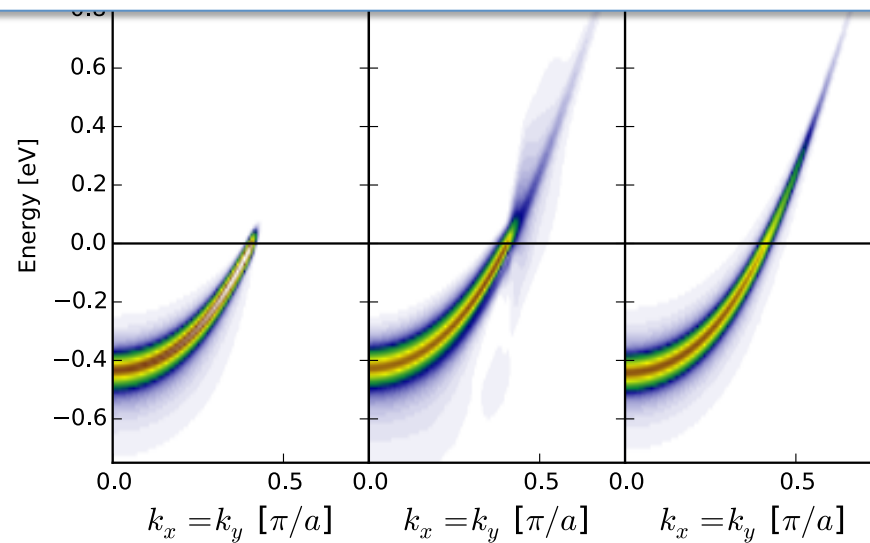


Electron-phonon



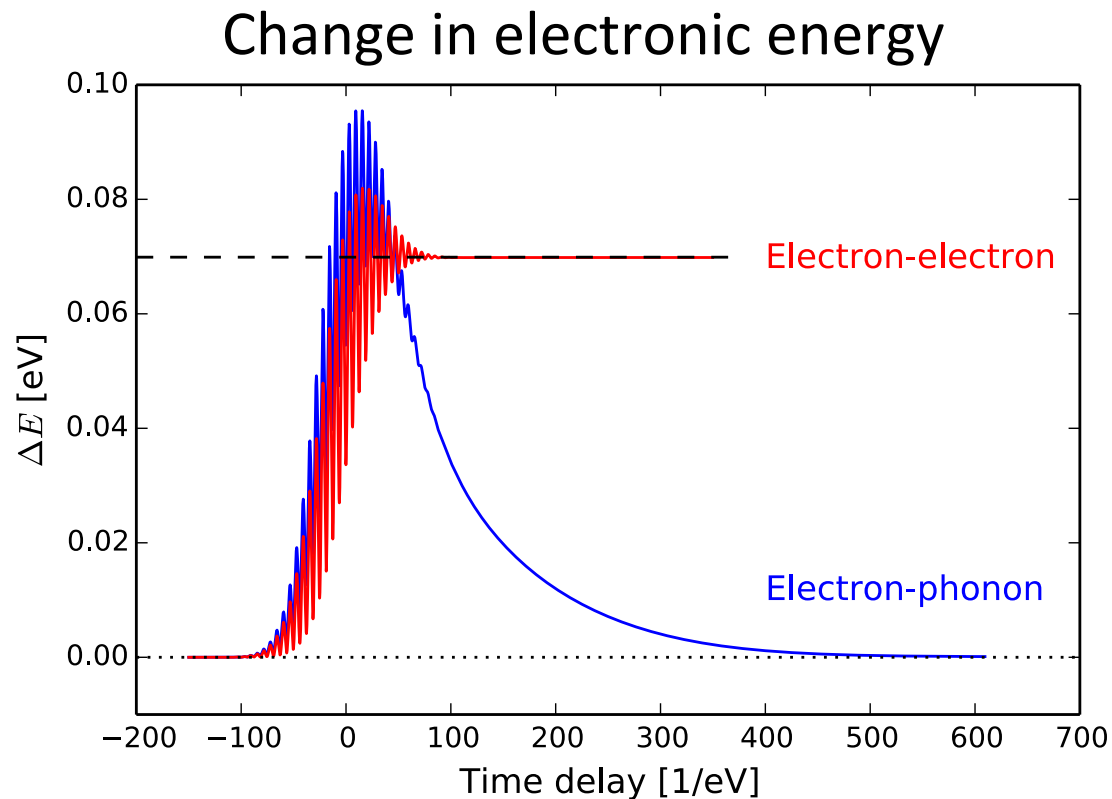
Let's consider the combination

Electron-electron

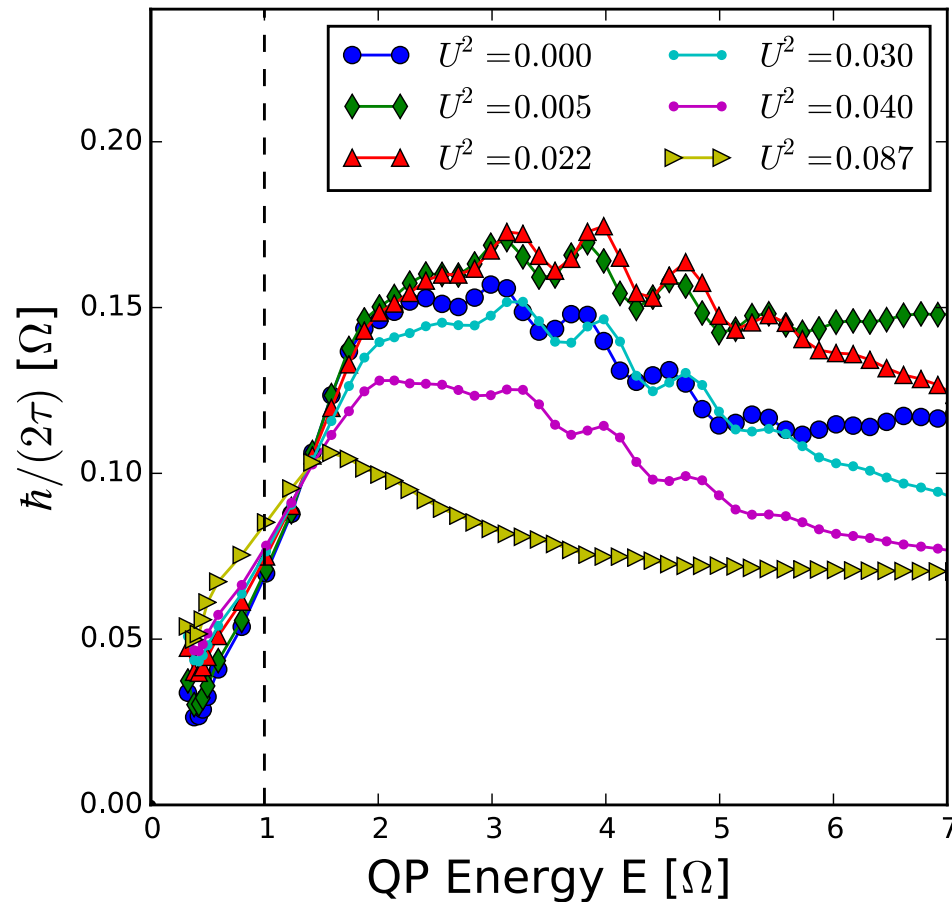


$$-2\text{Im}\Sigma(\omega = \epsilon_{\mathbf{k}}) \neq \frac{1}{\tau(\omega)}$$

**Energy transfer
determines
population dynamics**



Combining electron-electron and electron-phonon scattering



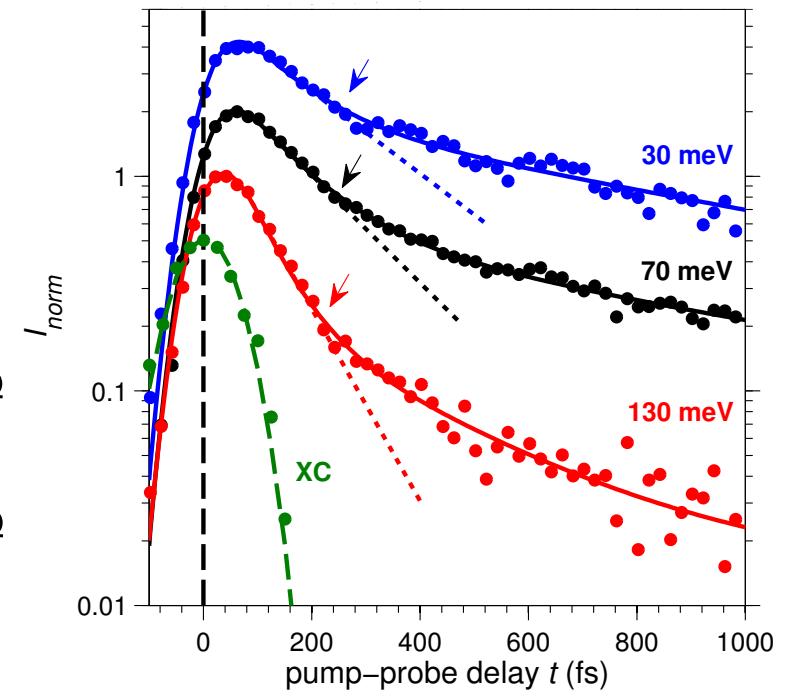
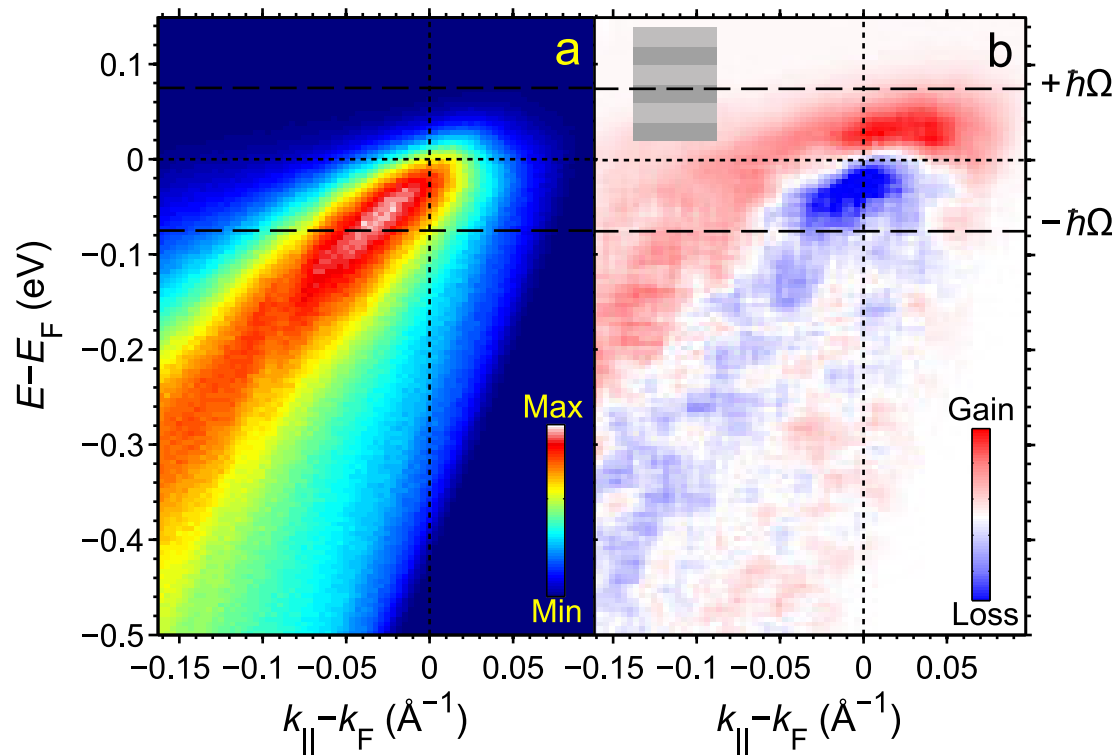
$$g^2 = 0.02$$

Step in lifetimes
remains visible

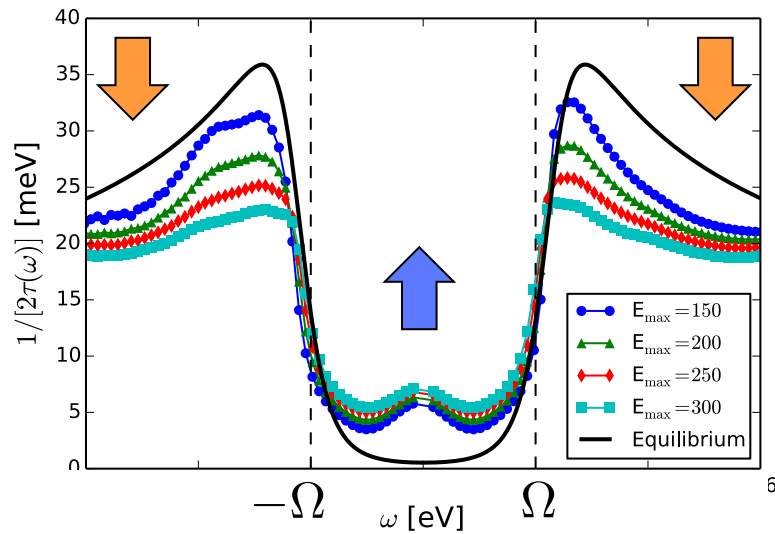
Competition
between e-p and e-e
scattering

Apparent λ could be
too small!

Time-resolved ARPES experiment by *J.D. Rameau, S. Freutel, I. Avigo, M. Ligges, L. Rettig, P.D. Johnson, U. Bovensiepen*

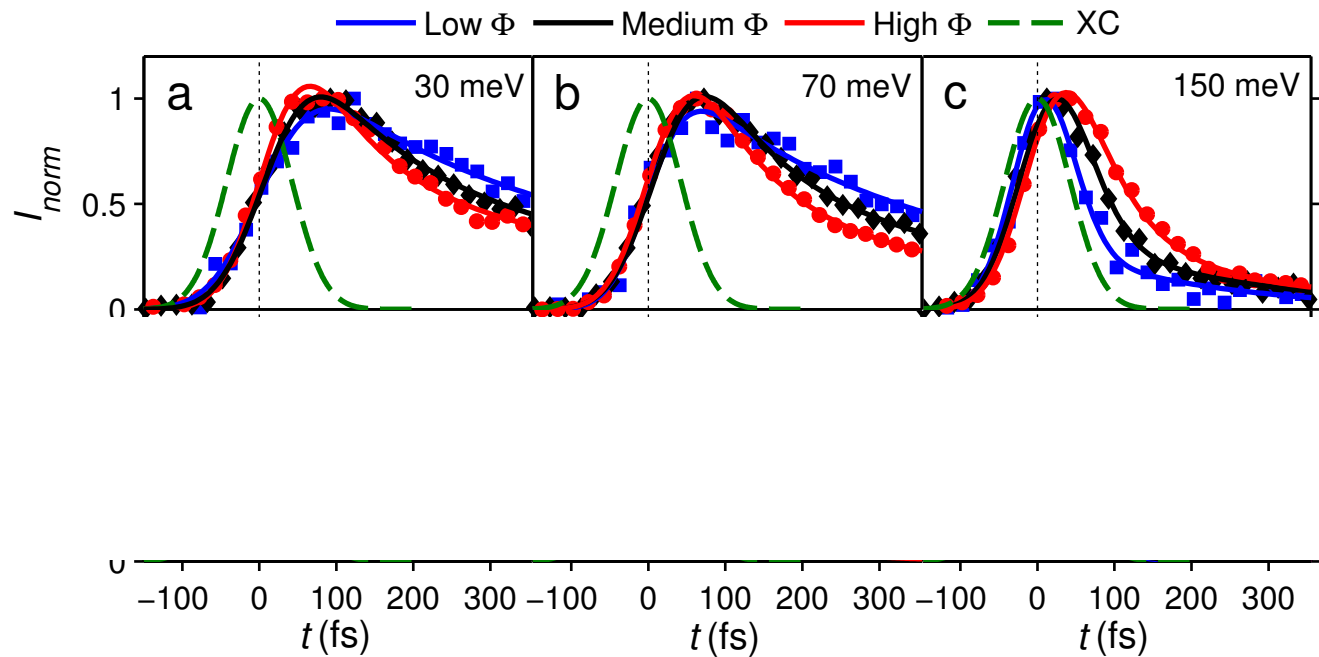


Population decay time in Bi2201 as a function of binding energy

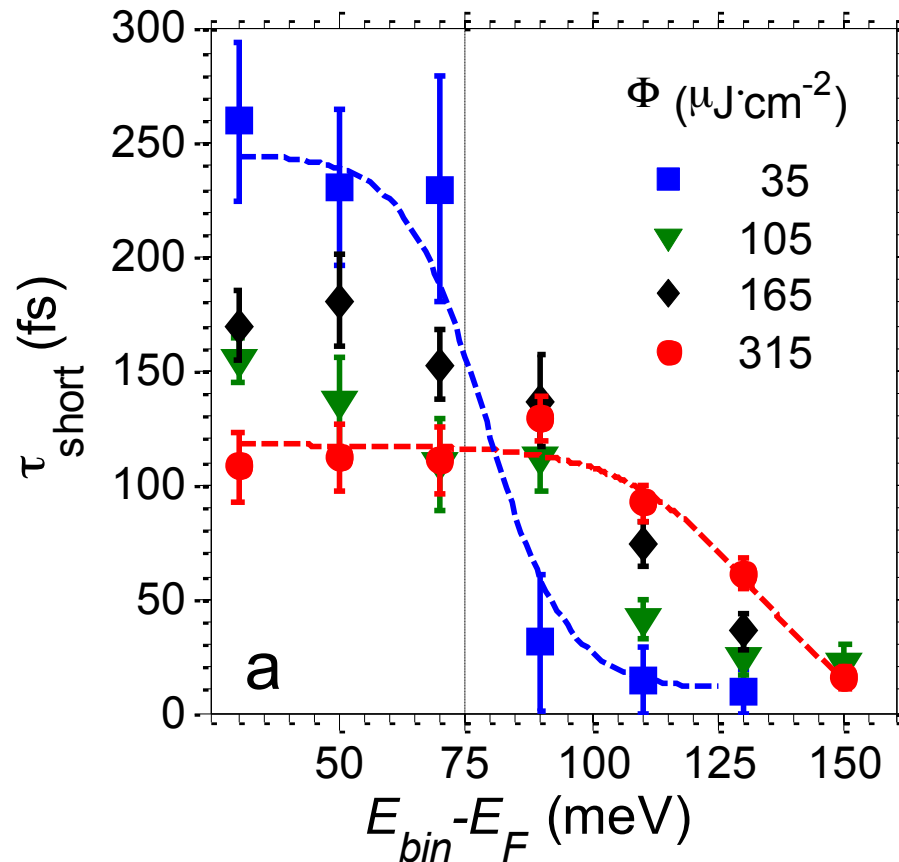


Scattering rates are fluence dependent

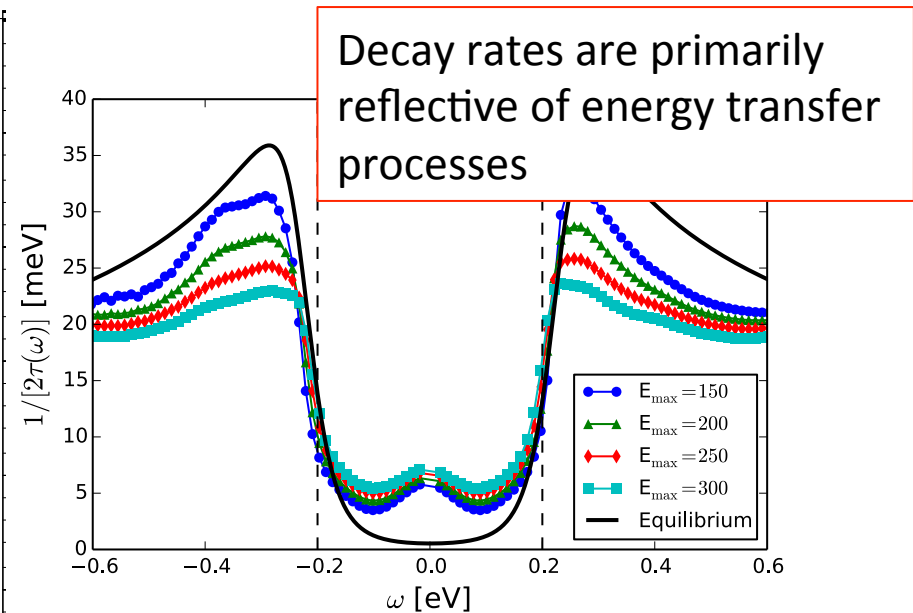
Experiment



Experiment

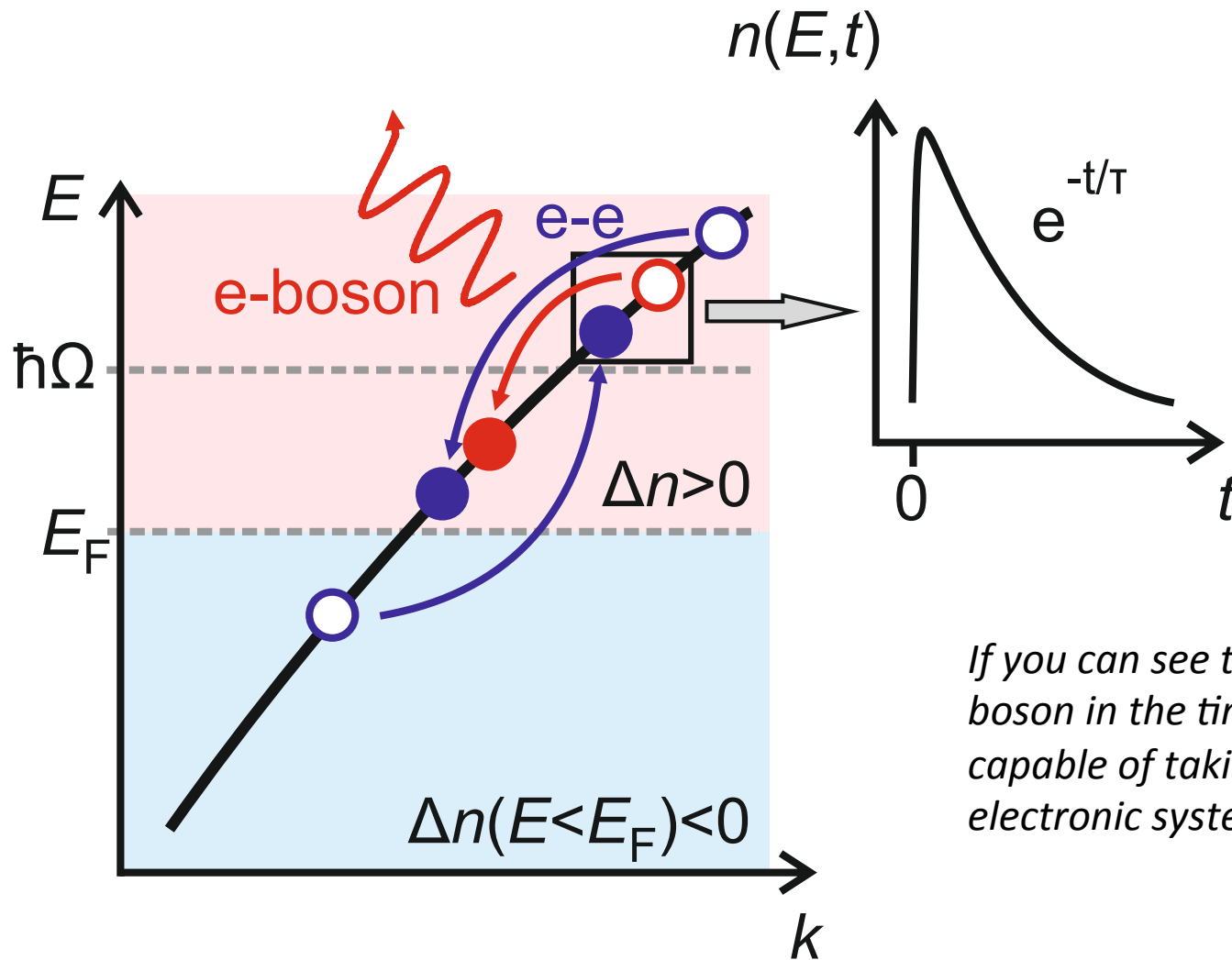


Theory



Population dynamics can be understood with a strongly coupled boson at approximately 75 meV and $\lambda \approx 0.2$

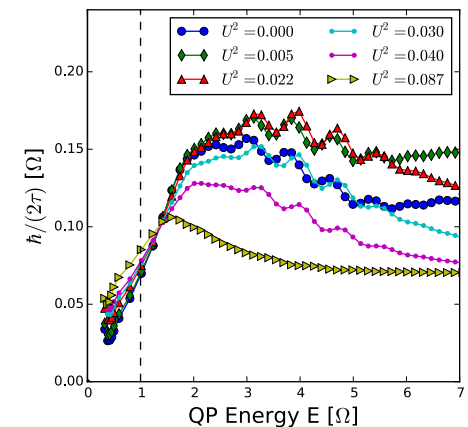
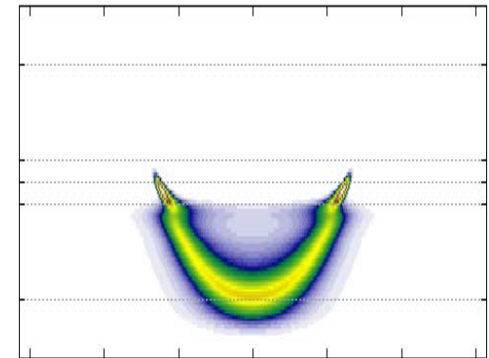
Quantitative agreement between experiment and theory



If you can see the fingerprint of a boson in the time domain, it is capable of taking energy out of the electronic system.

Summary

- Dynamics in the time domain are not always equivalent to frequency domain
- Dynamics in the time domain are principally controlled by energy transfer processes
 - We can use this to separate/suppress interactions that can obscure electron-boson interactions
- Interpreting changes in the spectra using equilibrium language can be erroneous



PRX 3, 041033 (2013)

PRB 87, 235139 (2013)

PRB 90, 075126 (2014)

arXiv:1505.07055 (updated tomorrow)